

Часть 1

Олимпиада: **Математика, 11 класс (1 часть)**

Шифр: **21104385**

ID профиля: **159158**

Вариант 21

№1

методом

21 вариант

Лист №1

a_1, a_2, \dots - арифметическая прогрессия

$a_n = a_1 + (n-1)d$, где d - разность прогрессии

$d > 0$, т.е. прогрессия возрастает $a_1 = ?$

d - целое, т.е. a_1, a_2, \dots - целые

$$(a_8 \cdot a_{17}) > S + 27$$

$$(a_{11} \cdot a_{14}) < S + 60$$

$$S = a_1 + a_2 + \dots + a_{27} =$$

$$= \frac{a_1 + a_{27}}{2} \cdot 27 = \frac{2a_1 + 6d}{2} \cdot 27 = 27a_1 + 27d$$

$$(a_1 + 7d)(a_1 + 16d) > 7a_1 + 27d + 27$$

$$(a_1 + 10d)(a_1 + 13d) < 7a_1 + 27d + 60$$

$$a_1^2 + 23da_1 + 112d^2 > 7a_1 + 27d + 27$$

$$7a_1 + 27d + 60 > a_1^2 + 23da_1 + 130d^2 \quad (+)$$

$$112d^2 + 60 > 130d^2 + 27$$

$$d^2 < \frac{33}{18} \quad \text{т.е. } d \text{ - целое и } d > 0 \Rightarrow d = 1$$

$$a_1^2 + 23a_1 + 112 > 7a_1 + 27 + 27$$

$$a_1^2 + 23a_1 + 130 < 7a_1 + 27 + 60$$

$$a_1^2 + 16a_1 + 64 > 0 \Rightarrow (a_1 + 8)^2 > 0 \Rightarrow a_1 \neq -8$$

$$a_1^2 + 16a_1 + 49 < 0$$

$$a_1^2 + 16a_1 + 49 < 0$$

$$D = 64 - 49 = 15$$

$$a_1 = -8 \pm \sqrt{15}$$

$$\Rightarrow a_1 \in (-8 - \sqrt{15}; -8 + \sqrt{15})$$

$$-12 < -8 - \sqrt{15} < -11 \quad \text{т.к. } a_1 \text{ - целое}$$

$$\Rightarrow a_1 \in \{-11\} \cup \{-10\} \cup \{-9\} \cup \{-7\} \cup$$

$$\cup \{-6\} \cup \{-5\}$$

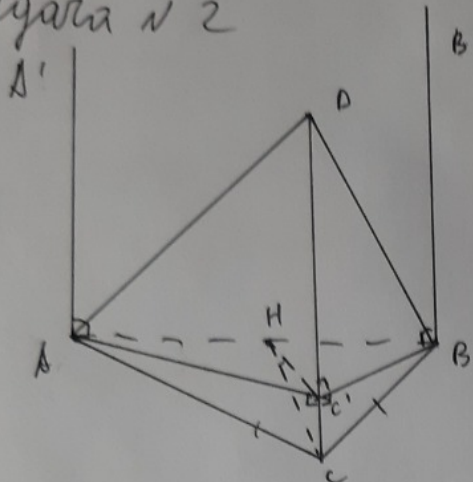
$$-5 < -8 + \sqrt{15} < -4$$

Ответ: $-11; -10; -9; -7; -6; -5$

Числовик

71 вариант
 $\Delta ACD \sim \Delta BCD$

Задача 12



Дано:

$ABCD$ - тетраэдр. висота h

$AB = 4$

$AC = CB = 5$

$AD = DB = 6$

R - осн - проекция.

\perp
 $CD = ?$

Решение:

$AA'; BB' \parallel CD \Rightarrow$ образующие цилиндра
 цилиндр - прямой \Rightarrow осн $\perp AA'$

$AC'B \perp AA' \Rightarrow \angle AC'C = \angle BC'C = 90^\circ$

$C' \in CD$

т.ч. CC' - общий к $AC = CB$

$\Delta AC'B$ - висота h

отрезки равны по определению

$\Delta AC'C \cong \Delta BC'C \Rightarrow AC' = BC'$

H - середина AB

т.ч. $AC' = C'B$

$CH \perp AB$

$Fh = 3x$

т.ч. $CC' \perp AC'B$

$CH \perp AB$

перпендикуляр.

$\angle CAB' = \angle C'AB = \angle C'HC = \alpha$

ΔBCH - прямоугольный $\Rightarrow CH = \sqrt{BC^2 - BH^2} = \sqrt{25 - 4} = \sqrt{21}$

Поэтому $R_{осн} = R_{\Delta AC'B} = \frac{AC' \cdot BC' \cdot AB}{4 S_{\Delta AC'B}}$

$C'H = CH \cdot \cos \alpha$ ($\angle CC'H = 90^\circ$)
 $= \sqrt{21} \cos \alpha$

$C'B = \sqrt{C'H^2 + HB^2} = \sqrt{21 \cos^2 \alpha + 4} = AC'$

$S_{\Delta AC'B} = \frac{1}{2} HC' \cdot AB = \frac{1}{2} \cdot 4 \cdot \sqrt{21} \cos \alpha = 2\sqrt{21} \cos \alpha$

Задача №2

Умножим

21 (вспомогат.)

Личи №3

$$R = \frac{AC' \cdot BC' \cdot AB}{4 S_{ABC'}} = \frac{(21 \cos^2 d + 4) \cdot 4}{4 \cdot 2\sqrt{21} \cos d} = \frac{\sqrt{21}}{2} \cos d + \frac{2}{\sqrt{21} \cos d}$$

$$R'(d) = -\frac{\sqrt{21}}{2} \sin d + \frac{2}{\sqrt{21}} \left(\frac{-\sin d}{\cos^2 d} \right) = \frac{2}{\sqrt{21}} \frac{\sin d}{\cos^2 d} - \frac{\sqrt{21}}{2} \sin d = 0$$

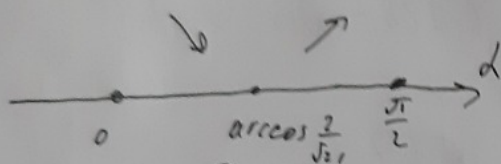
$$\sin d = 0 \Rightarrow d = 0$$

$$\cos^2 d = \frac{4}{21}$$

$$\cos d = \frac{2}{\sqrt{21}} \Rightarrow d = \arccos \frac{2}{\sqrt{21}}$$

$$\sin d (4 - 21 \cos^2 d) = 0$$

$$d \in [0; \frac{\pi}{2}]$$



~~$$R(0) = \frac{\sqrt{21}}{2} + \frac{2}{\sqrt{21}} = \frac{23}{2\sqrt{21}}$$~~

$$R(\arccos \frac{2}{\sqrt{21}}) = 1 + 1 = 2$$

$$R(0) > R(\arccos \frac{2}{\sqrt{21)}) \Leftrightarrow$$

$$2 < \frac{23}{2\sqrt{21}}$$

$$4\sqrt{21} < 23 \quad | \cdot 2$$

$$16 \cdot 21 < 23 \cdot 23$$

$$d = \arccos \frac{2}{\sqrt{21}}$$

$$\cos d = \frac{2}{\sqrt{21}} \Rightarrow \sin d = \frac{\sqrt{17}}{\sqrt{21}} \Rightarrow CC' = CH \cdot \sin d = \sqrt{17}$$

~~$$DH = \sqrt{D}$$~~

DH - высота в $\triangle ADB$ т.е. $AP = DB$

$$DH = \sqrt{DB^2 - HB^2} = \sqrt{36 - 4} = 4\sqrt{2}$$

$\triangle DC'H$ - прямоугол. $C'H \perp DC'$ ($AC'B \perp C'D$)

$$C'D = \sqrt{DH^2 - C'H^2} = \sqrt{32 - 4} = 2\sqrt{7}$$

$$C'H = \sqrt{21} \cos d = 2$$

Числові

Задача №2

21 варчанти

листі №4

C' є на відрітку DC

C' може знаходитись як між DC , так і за C

1) C' між DC

$$CD = CC' + C'D = \sqrt{17} + 2\sqrt{7}$$

2) C' за C

$$CD = C'D - CC' = 2\sqrt{7} - \sqrt{17} > 0 \quad (\sqrt{28} - \sqrt{17} > 0)$$

Відповідь: $\sqrt{17} + 2\sqrt{7}$; $2\sqrt{7} - \sqrt{17}$

Задача №3

Условие

Лист №5

$$(x-a)^2 + (y-b)^2 \leq 20$$

$(a; b)$ - центр окруж.

с радиусом $\sqrt{20}$

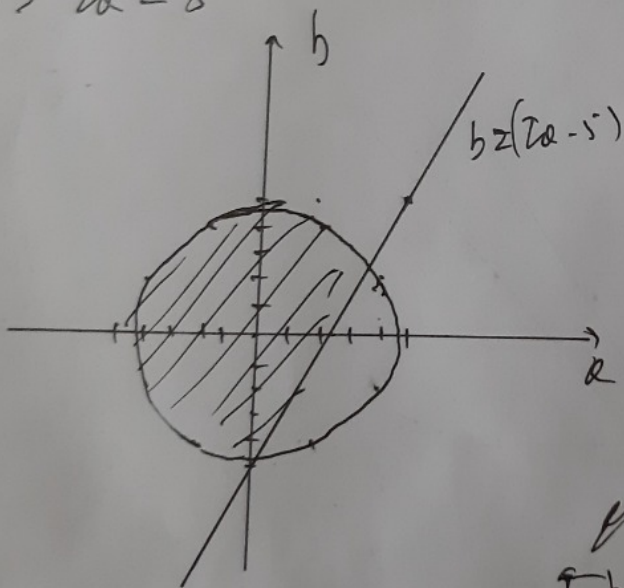
$$a^2 + b^2 \leq \min(8a - 4b; 20)$$

$$a^2 + b^2 \leq \min(8a - 4b; 20)$$

1) $8a - 4b \geq 20$

$a^2 + b^2 \leq 20$ ^{центр} ~~центр~~ $P = \sqrt{20}$
 $C_y = (0; 0)$

$b > 2a - 5$



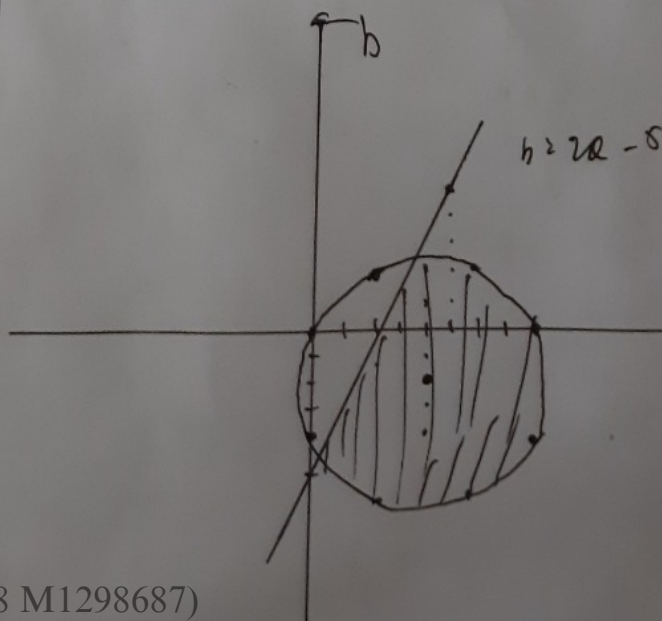
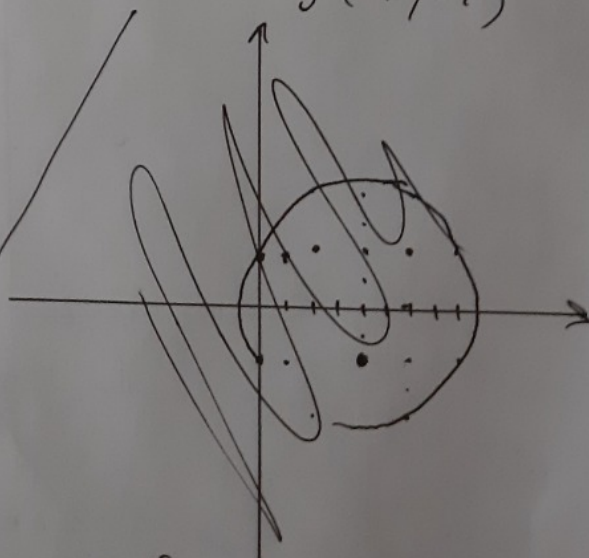
2) $8a - 4b \geq 20$

$b < 2a - 5$

$a^2 + b^2 \leq 8a - 4b$

$(a-4)^2 + (b+2)^2 \leq 20$

или ^{центр} $P = \sqrt{20}$
 $C_y = (4; -2)$



с центром $(4; -2)$
 - координаты
 центра окруж.
 $(x-a)^2 + (y-b)^2 \leq 20$

Задача № 3

Знаем, что M - пересечение двух
 кругов с радиусами 20 и центрами
 (0; 0) и (4; -2) (т.е. a и b это x и
 y центров кругов R=20)

$$\begin{cases} x^2 + y^2 = 20 \\ y = 2x - 5 \end{cases}$$

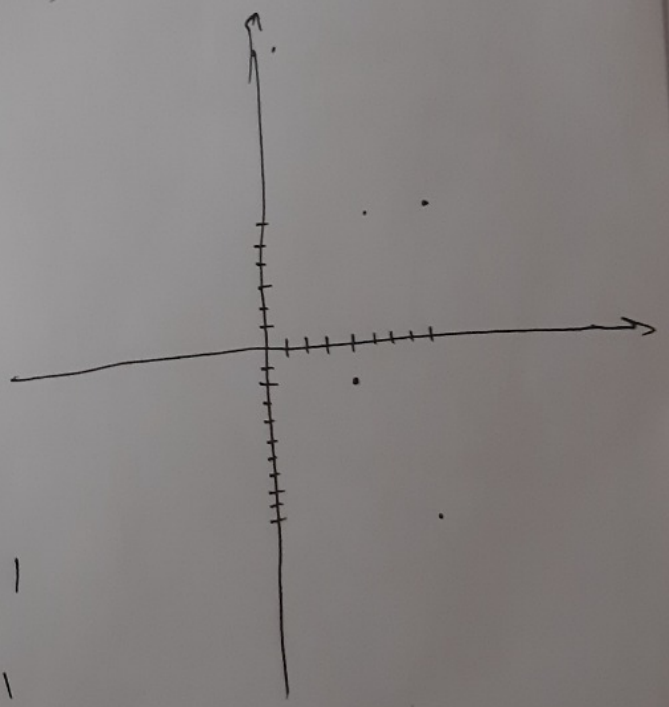
$$\begin{aligned} x^2 + 4x^2 - 20x + 25 &= 20 \\ 5x^2 - 20x + 5 &= 0 \\ x^2 - 4x + 1 &= 0 \end{aligned}$$

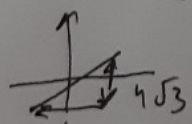
$$D = 4 - 1 = 3$$

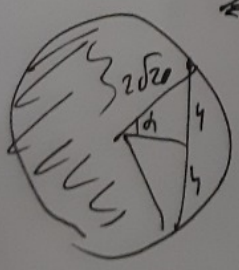
$$x_{1,2} = 2 \pm \sqrt{3}$$

$$x_1 = 2 + \sqrt{3} \quad y_1 = 2\sqrt{3} - 1$$

$$x_2 = 2 - \sqrt{3} \quad y_2 = -2\sqrt{3} - 1$$



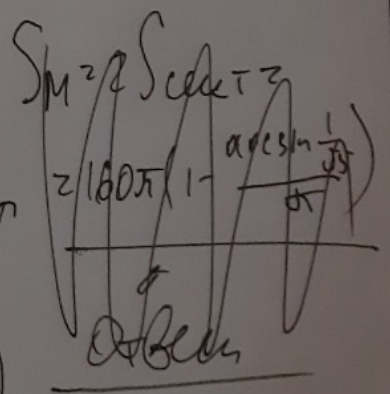
Сторона =  \Rightarrow $l_{\text{гипот}} = \sqrt{16 + 16 \cdot 3} = 8$



$$\sin \alpha = \frac{4}{20} = \frac{1}{5} \Rightarrow \alpha = \arcsin\left(\frac{1}{5}\right)$$

$$S_{\text{сект}} = \frac{1}{2} R^2 \alpha$$

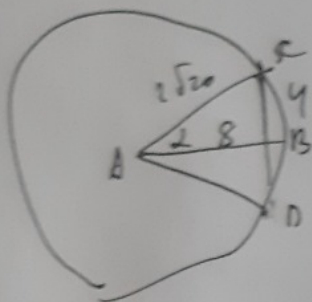
$$= \pi R^2 \left(1 - \frac{\alpha}{2\pi}\right) = \pi \cdot 80 \left(1 - \frac{\arcsin\left(\frac{1}{5}\right)}{\pi}\right)$$



Задача №3 Умножить числа

$$S_M = 2S_{\text{сектор}} + 2S_{\Delta} =$$

$$= 160\pi \left(1 - \frac{\arcsin \frac{1}{\sqrt{5}}}{\pi}\right) + 64$$

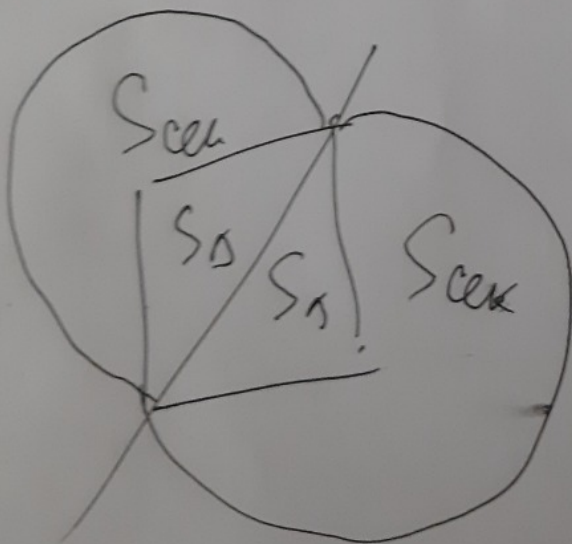


$$S_{ABD} = 2S_{ABC} =$$

$$S_D = S_{ACD}$$

$$AB = \sqrt{80 - 16} = 8$$

$$S_{ACB} = \frac{8 \cdot 8}{2} = 32$$



Ответ:

$$160\pi \left(1 - \frac{\arcsin \frac{1}{\sqrt{5}}}{\pi}\right) + 64$$

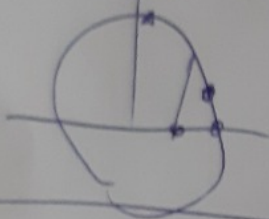
$$\frac{f(x)}{g(x)} = \frac{f'(x) \cdot g(x) - g'(x) \cdot f(x)}{g'(x)^2}$$

Uppräknat
 $x^2 = 2x$

$$= \frac{+\sqrt{21} \sin d \cdot 2}{21 \cos^2 d}$$

$$\frac{2}{\sqrt{21} \cos d} = \frac{2}{\sqrt{21}} (\cos d)^{-1} = + \frac{2 \cdot \cos^2 d}{\sqrt{21} \cdot \sin d}$$

$$\cos d = \frac{1}{2}$$



$$R = \frac{\sqrt{21}}{2} \cos d + \frac{2}{\sqrt{21} \cos d}$$

$$\cos d = \frac{2}{\sqrt{21}}$$

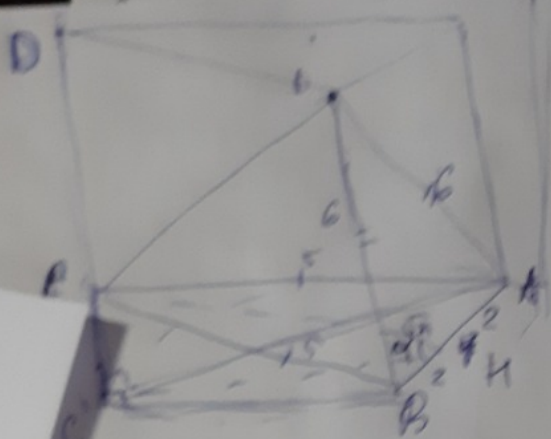
$$R = 1 + 2 \text{ (2)}$$

$$\sin d = 0 = \cos d = 1$$

$$R = \frac{\sqrt{21}}{2} + \frac{2}{\sqrt{21}} = \frac{21 + 2}{2\sqrt{21}} = \frac{23}{2\sqrt{21}}$$

$$\cos d = \frac{2}{\sqrt{21}}$$

$$\begin{array}{l} \frac{23}{2\sqrt{21}} \text{ (2)} \\ \frac{23}{12} \rightarrow 4\sqrt{21} \\ 93 \cdot 23 \rightarrow 16 \cdot 21 \end{array}$$



$R = \frac{abc}{4S}$ *Upramban*

$$= \frac{C'B \cdot C'A \cdot AB}{4 \cdot \frac{1}{2} C'A \cdot C'B \cdot \sin \angle C'B}$$

$$= \frac{AB}{2 \sin \angle C'B}$$

$(C'B = C'A)$ *Persegi!*

~~$R = \frac{abc}{4S}$~~

$$R = \frac{C'B \cdot C'A \cdot AB}{4S_{C'BA}}$$

$$CH = \sqrt{25 - 4} = \sqrt{21}$$

$$C'H = \sqrt{21} \cos \alpha$$

~~$$S_{ABC} \cdot \cos \alpha =$$~~

$$S_{ABC} =$$

$$\sqrt{21 \cos^2 \alpha + 4} = BC'$$

$$R = \frac{(21 \cos^2 \alpha + 4) \cdot \sqrt{21}}{\sqrt{21} \cdot \frac{1}{2} \cdot 4 \cdot \sqrt{21} \cos \alpha}$$

$$= \frac{21 \cos^2 \alpha + 4}{2\sqrt{21} \cos \alpha} = \frac{\sqrt{21}}{2} \cos \alpha + \frac{2}{\sqrt{21} \cos \alpha}$$

Derivasi

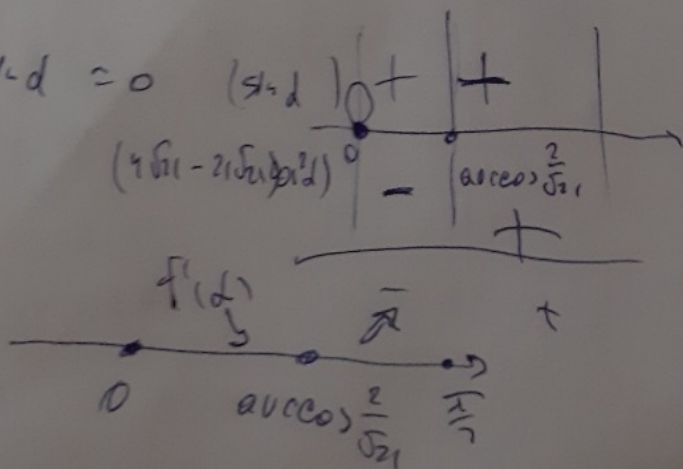
$$R'(\alpha) = -\frac{\sqrt{21}}{2} \sin \alpha + \frac{2\sqrt{21} \sin \alpha}{21 \cos^2 \alpha} = 0$$

$$4\sqrt{21} \sin \alpha - 21\sqrt{21} \cos^2 \alpha - \sin \alpha = 0 \quad (\sin \alpha) \quad \begin{array}{|c|c|} \hline + & + \\ \hline \end{array}$$

$$4\sqrt{21} - 21\sqrt{21} \cos^2 \alpha = 0 \quad (4\sqrt{21} - 21\sqrt{21} \cos^2 \alpha) \quad \begin{array}{|c|c|} \hline - & \arccos \frac{2}{\sqrt{21}} \\ \hline \end{array}$$

$$\cos^2 \alpha = \frac{4}{21}$$

$$\cos \alpha = \frac{2}{\sqrt{21}}$$



~~Умножение~~ Умножение

Задача №3.

$$\begin{cases} (x-a)^2 + (y-b)^2 \leq 20 \\ a^2 + b^2 \leq \min(8a-4b; 20) \end{cases}$$

$(x-a)^2 + (y-b)^2 \leq 20$ - круг с радиусом $2\sqrt{5}$

$$a^2 + b^2 \leq \min(8a-4b; 20)$$

1) $8a-4b > 20$

2) $8a-4b \leq 20$

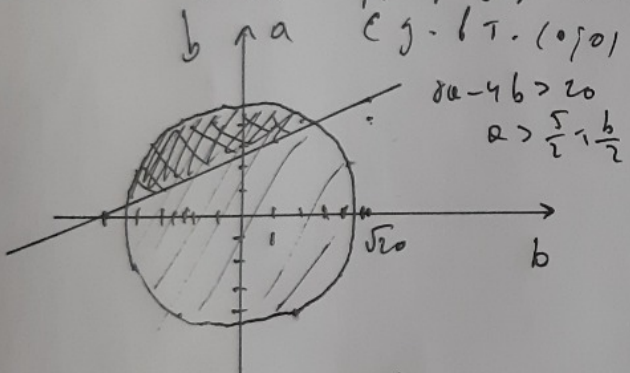
$$a \leq \frac{5}{2} + \frac{b}{2}$$

$a^2 + b^2 \leq 20$ - круг радиуса $\sqrt{20}$

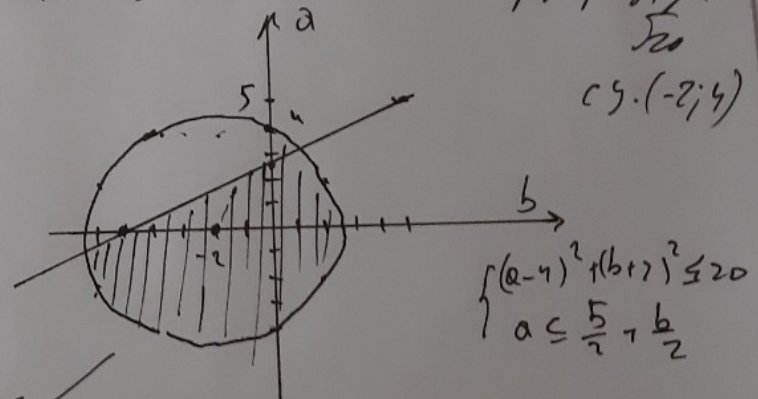
$$a^2 + b^2 \leq 8a - 4b$$

$$a^2 - 8a + 16 + b^2 + 4b + 4 \leq 20$$

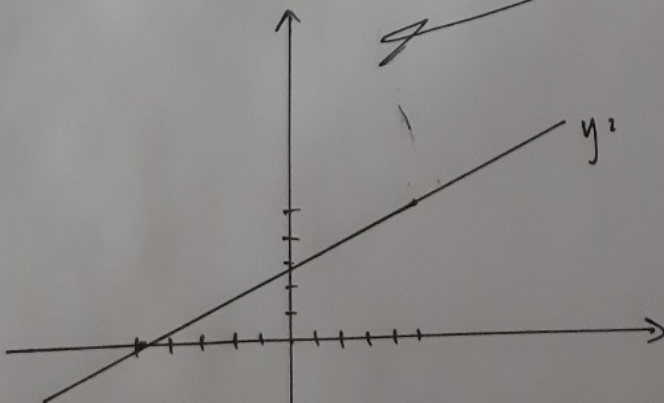
$(a-4)^2 + (b+2)^2 \leq 20$ - круг радиуса $\sqrt{20}$



$$\begin{aligned} 8a - 4b &> 20 \\ a &> \frac{5}{2} + \frac{b}{2} \end{aligned}$$

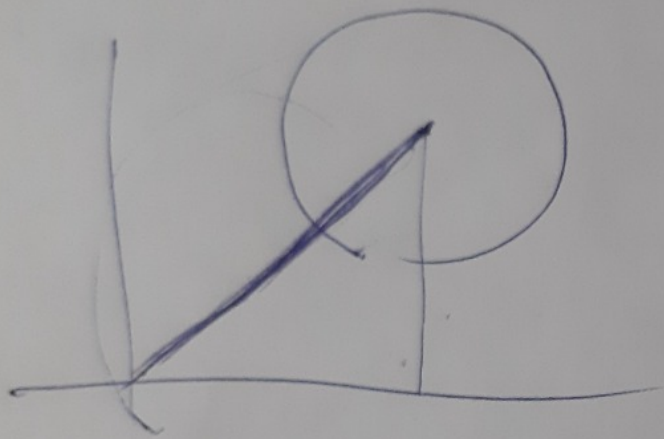


$$\begin{cases} (a-4)^2 + (b+2)^2 \leq 20 \\ a \leq \frac{5}{2} + \frac{b}{2} \end{cases}$$



$$\begin{cases} (x-a)^2 + (y-b)^2 \leq 20 \\ a^2 + b^2 \leq \min(8a - 4b, 20) \end{cases}$$

Упроблема.

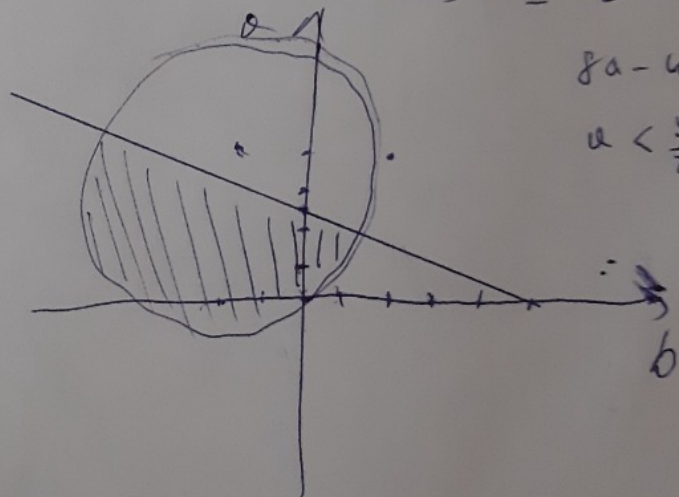


$$a^2 + b^2 \leq 8a - 4b$$

$$a^2 - 8a + b^2 - 4b \leq 0$$

$$a^2 - 8a + 16 + b^2 - 4b + 4 \leq 20$$

$$(a-4)^2 + (b+2)^2 \leq 20$$



$$8a - 4b < 20$$

$$a < \frac{5}{2} - \frac{b}{2}$$

Часть 2

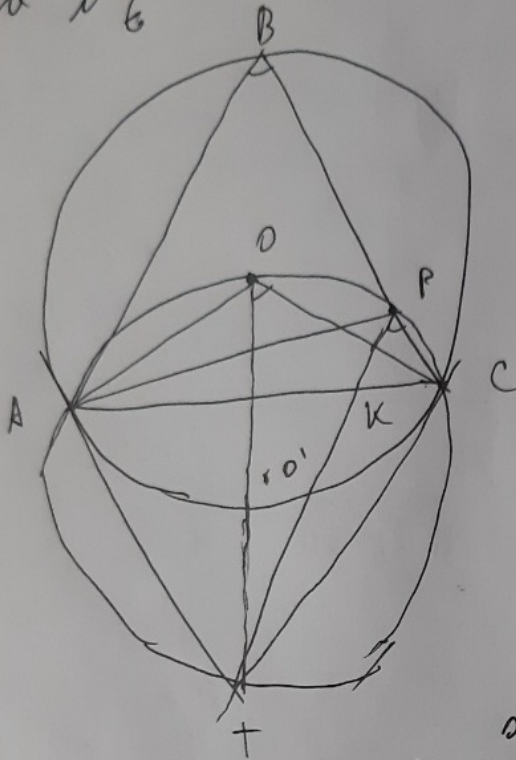
Олимпиада: **Математика, 11 класс (2 часть)**

Шифр: **21104385**

ID профиля: **159158**

Вариант 21

Задача № 6



Решение

$$\angle OAT + \angle OCT = 180^\circ \quad (\text{AT и CT - кас-ел})$$

$\Delta OATC$ - вписан в $\omega'(O')$

$T \in \omega'$
 π -угол $\angle ABC = 2d \Rightarrow$

$$\Rightarrow \angle AOC = 2d$$

$$\text{т.к. } AO = OC$$

OT - ось.

$$\angle OAT = \angle OCT = 90^\circ$$

$\Delta OAT \sim \Delta OCT$ *по теореме*

$$\angle OPT = d \Rightarrow \angle CPT = d$$

$$\frac{S_{APK}}{S_{PKC}} = \frac{AK}{KC} = \frac{12}{y} = \frac{4}{3} \Rightarrow \frac{KC}{AC} = \frac{3}{7} \Rightarrow KC = \frac{3}{7} AC$$

$\Delta PKC \sim \Delta BAC$ т.к. $\angle C$ - общий; $\angle ABC = \angle KPC$

$$\frac{S_{ABC}}{S_{PKC}} = \left(\frac{AC}{KC}\right)^2 \Rightarrow \boxed{S_{ABC} = 9 \cdot \frac{49}{9} = 49} \quad (1)$$

$\angle APC = \angle AOP = 2d$, $\angle FPC = d \Rightarrow \text{Ph-центр } \angle APC \Rightarrow$

$$\Rightarrow \frac{PC}{AP} = \frac{KC}{AK} = \frac{3}{4} \Rightarrow PC = 3y$$

$$AP = 4y \Rightarrow S_{APC} = \frac{1}{2} \sin 2d \cdot AP \cdot PC = 6y^2 \sin 2d = 25$$

$$y^2 = \frac{25}{6 \sin 2d} = \frac{7}{2 \sin 2d} \quad (S_{APK} + S_{PKC} = 12 + 9 = 21)$$

По теореме косинусов $\angle APC$

$$AC^2 = AP^2 + PC^2 + 2 \cos 2d \cdot AP \cdot PC = 25y^2 + 2 \cos 2d \cdot 12y^2 =$$

$$= \frac{7}{6 \sin 2d} (25 + 24 \cos 2d)$$

Учтобен

Лист № 3

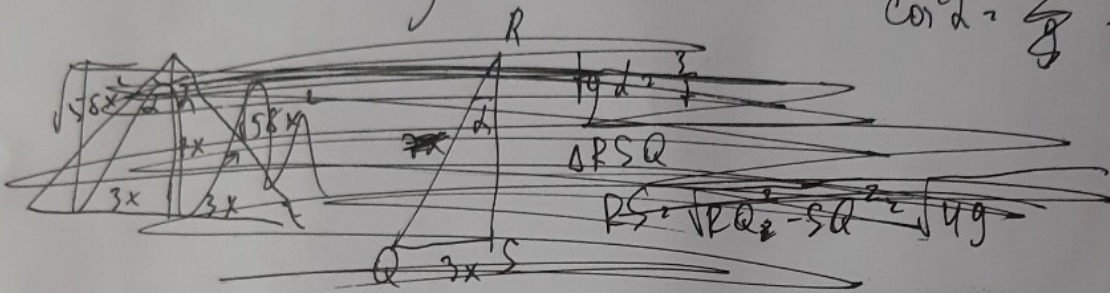
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Задача

№ 6.

$$AC = \sqrt{\frac{F}{2 \sin^2 d}} (25 - 24 \cos^2 d)$$

$$d = \angle ABC = \arctan \frac{3}{7}$$



$$\frac{9}{49} + 1 = \frac{1}{\cos^2 d}$$

$$\frac{9}{49} + 1 = \frac{1}{\cos^2 d}$$

$$\cos^2 d = \frac{49}{58}$$

$$\cos d = \frac{7}{\sqrt{58}}$$

$$\Rightarrow \sin d = \frac{3}{\sqrt{58}}$$

$$\Rightarrow \sin 2d = 2 \sin d \cdot \cos d = \frac{42}{58}$$

$$AC = \sqrt{\frac{F \cdot 29}{2 \cdot 21}} \left(25 - \frac{24 \cdot 20}{29} \right) =$$

$$= 7 \sqrt{\frac{5}{6}} = 7 \sqrt{\frac{5}{6}}$$

$$\begin{aligned} \cos^2 d &= 2 \cos^2 d - 1 \\ &= \frac{21}{29} \\ &\Rightarrow \frac{49}{29} - 1 = \frac{20}{29} \end{aligned}$$

Отвеч: а) 49 ; б) $7 \sqrt{\frac{5}{6}}$

N 5

Умножим

ЛУСТ N 1

216

$$a = \log_{\sqrt{2x-3}}(x+1), \quad b = \log_{2x^2-3x+5}(2x-3)^2, \quad c = \log_{(x+1)}(2x^2-3x+5)$$

$$\text{OD3: } 2x-3 > 0 \\ x > \frac{3}{2} \\ 2x-3 \neq 1 \\ x \neq 2$$

$$2x^2-3x+5 > 0 \\ D = 9 - 40 < 0$$

$$2x^2-3x+5 \neq 1 \\ 2x^2-3x+4 = 0 \\ D = 9 - 48 < 0$$

$$\left. \begin{array}{l} a \neq 0 \\ b \neq 0 \\ c \neq 0 \end{array} \right\}$$

$$x \in \left(\frac{3}{2}; 2\right) \cup (2; \infty)$$

В П-ТБ где мы можем a; b; c равны d, тогда третье равно (d-1)

$$a \cdot b \cdot c = d^2(d-1)$$

$$\log_{\sqrt{2x-3}}(x+1) \cdot \log_{2x^2-3x+5}(2x-3)^2 \cdot \log_{(x+1)}(2x^2-3x+5) = d^2(d-1)$$

$$\frac{1}{2} \neq \log_{2x^2-3x+5}(x+1) \cdot \log_{(x+1)}(2x^2-3x+5) = d^2(d-1)$$

$$4 = d^3 - d^2 \Rightarrow d^3 - d^2 - 4 = 0 \quad d^3 - 2d^2 + d^2 - 4 =$$

$$= (d-2)d^2 + (d-2)d + 2 = (d-2)(d^2 + d + 2) = 0 \\ D < 0$$

$$d = 2$$

1) П-ТБ a = 2

$$\log_{\sqrt{2x-3}}(x+1) = 2$$

$$x+1 = 2x-3$$

$$x = 4$$

2) П-ТБ b = 2

$$\log_{2x^2-3x+5}(2x-3)^2 = 2$$

$$2x-3 = 2x^2-3x+5$$

$$2x^2-5x+8 = 0$$

$$D = 25 - 64 < 0$$

∅

3) П-ТБ c = 2

$$\log_{(x+1)}(2x^2-3x+5) = 2$$

$$2x^2-3x+5 = x^2+2x+1$$

$$x^2-5x+4 = 0$$

$$x = \int_1^4$$

1

$$\text{при } x = \frac{1}{4}$$

$$\Rightarrow \log_{2x^2-3x+5}(2x-3)^2 = 1$$

$$0 = c = 2$$

$$2x^2-3x+5 = 4x^2-12x+9 \Rightarrow$$

$$21104385 (U159158 M11208689) x+4=0$$

$$\text{при } x = 4 \quad f(x) = 0$$

X = 4
Отв: 4

AC-?

OT=20
OC=R
 $\cos d = \frac{R}{20}$

Uppuram

$\frac{20}{\sin d} = \frac{R}{\sin 2d}$

$\frac{AC}{\sin d} = 20$ $\frac{AC}{\sin 2d} = 20$

$\frac{\sin 2d}{\sin d} = \frac{R}{20}$

$441 + 400 \cos 2d = \frac{R}{\sin d}$

$841 + 400 \cos 2d = \frac{R}{\sin d}$

$\frac{1}{2} \sin 2d \cdot 24y^2 = 6y^2 \sin 2d = 15$

$y^2 = \frac{5}{2 \sin 2d}$

$AC^2 = AD^2 + PC^2 - 2 \cos 2d \cdot AP \cdot PC =$

$= 25y^2 - 2 \cos 2d \cdot 12y^2 =$

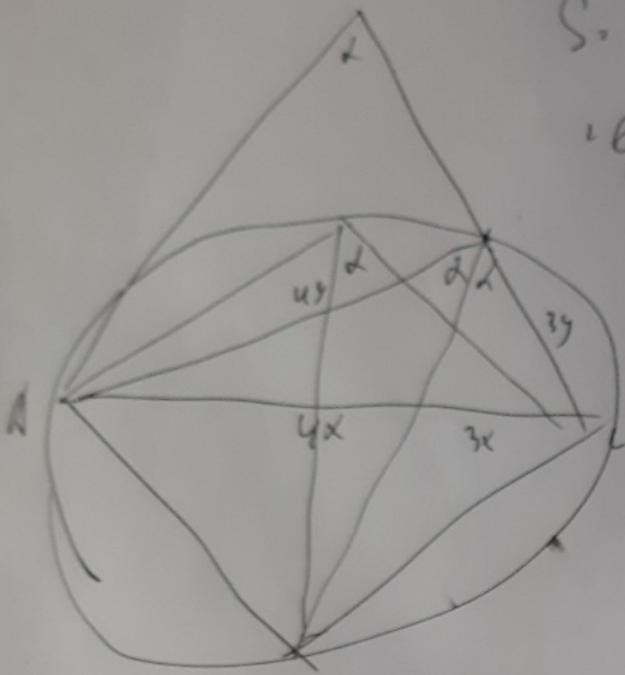
$2y^2 (25 - 24 \cos 2d) = \frac{5}{2 \sin 2d} (25 - 24 \cos 2d)$

$a \cdot a (a-1) = a^3 - a^2$

Uppuram

$(2a^2 - 3 \times 5)$

$\log (x+1) = \log (x+3)$



$$S = 15 = \frac{1}{2} \sin 2\alpha \cdot 12y^2$$

$$16y^2 \cdot \sin 2\alpha$$

$$4e^2 = 25y^2 - 2 \cos 2\alpha \cdot 12y^2$$

$$= y^2 (25 - 24 \cos 2\alpha) =$$

$$= \frac{5}{2 \sin 2\alpha} (25 - 24 \cos 2\alpha)$$

$$\tan \alpha = \frac{3}{7}$$

$$\tan^2 \alpha + 1 = \frac{1}{\cos^2 \alpha}$$

$$\frac{9}{49} + 1 = \frac{1}{\cos^2 \alpha}$$

$$\Rightarrow \cos \alpha = \frac{7}{\sqrt{58}}$$

$$\sin \alpha = \frac{3}{\sqrt{58}}$$

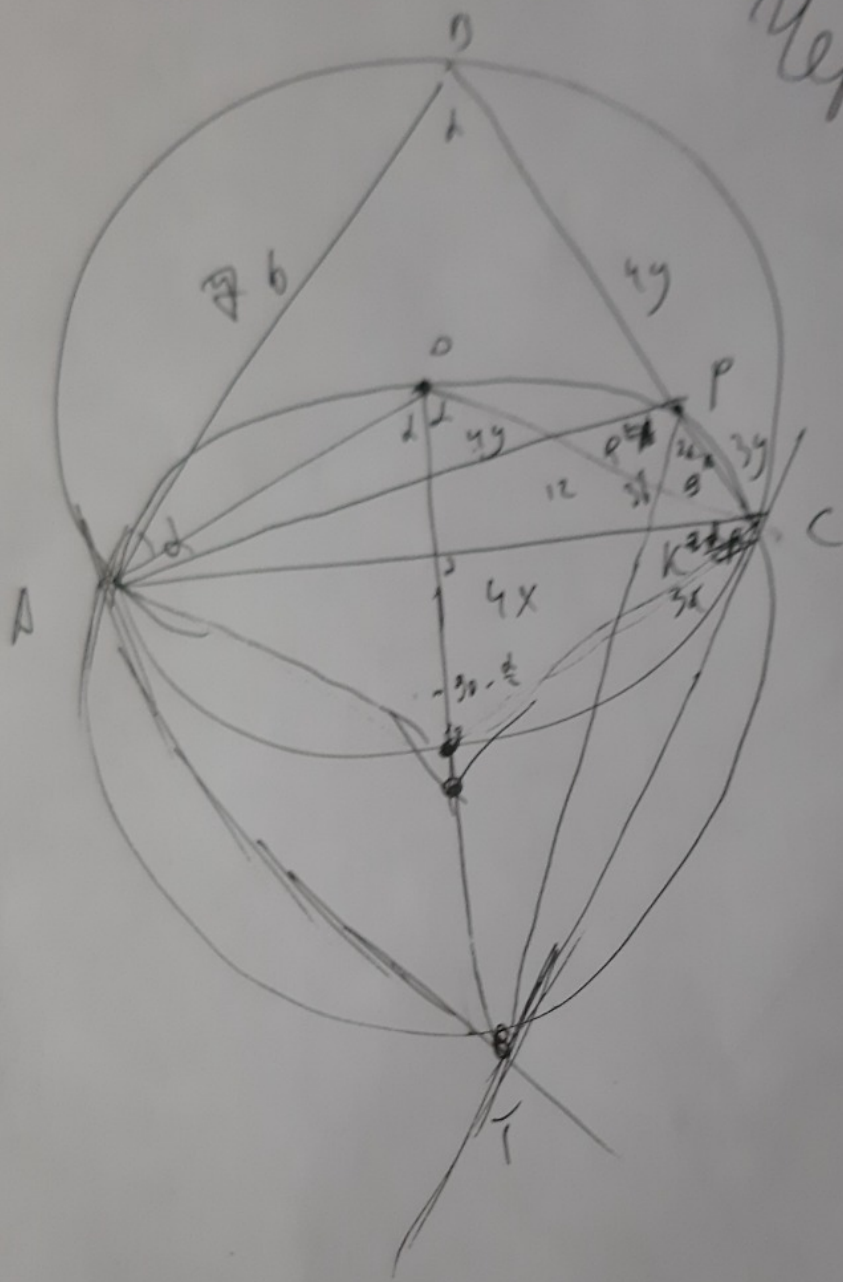
$$\sin 2\alpha = \frac{42}{58} = \frac{21}{29}$$

$$\cos 2\alpha = 2 \cos^2 \alpha - 1 = \frac{49}{29} - 1 = \frac{20}{29}$$

$$\sqrt{\frac{5 \cdot 29}{2 \cdot 21} \left(25 - \frac{24 \cdot 20}{29} \right)} = \sqrt{\frac{5 \cdot 29 \cdot 35}{2 \cdot 21}} = \sqrt{\frac{5^2 \cdot 7}{2 \cdot 3}} = 5 \sqrt{\frac{7}{6}}$$

245/2

$$\begin{array}{r} 25 \\ \times 29 \\ \hline 225 \\ + 50 \\ \hline 225 \\ - 450 \\ \hline 345 \end{array}$$



Упругий.

$$P_2 = \frac{514d}{2} \cdot 36 \cdot 39$$

$$S_2 = \frac{514 \cdot 2d}{2} \cdot 39 \cdot 49 = 215$$