

Часть 1

Олимпиада: **Физика, 11 класс (1 часть)**

Шифр: **21200737**

ID профиля: **342273**

Вариант 1

$$T \sin \alpha = mg - ma \sin \beta$$

$$T \cos \alpha = ma \cos \beta$$

$$\tan \alpha = \frac{g - a \sin \beta}{a \cos \beta}$$

$$\tan \beta = 2$$

$$\tan \alpha = \frac{5}{3} \quad \frac{4}{5} = \frac{4}{3}$$

$$\frac{8}{3} + 1$$

$$\frac{11}{3}$$

$$2 \frac{1}{\sqrt{5}}$$

$$2 - \frac{6}{5}$$

$$\frac{10-6}{5} = \frac{2}{5}$$

$$\frac{4}{3} \frac{1}{\sqrt{5}} + \frac{2}{\sqrt{5}}$$

$$\frac{4 - 3\sqrt{5}}{2}$$

$$\frac{2 \frac{T_0^2}{4} - \frac{3T_0^2}{2} + T_0^2}{2T_0}$$

$$\frac{9}{16} - \frac{9}{8} + \frac{1}{2}$$

$$\frac{625}{579}$$

$$\frac{9}{16} - \frac{9}{8} + \frac{8}{16}$$

$$\frac{91}{17-18} = \frac{91}{-1}$$

$$\frac{2}{3} + \frac{1}{3}$$

$$\frac{3}{2} + \frac{3}{2}$$

$$\frac{g \alpha \cos \beta + \pi}{g \alpha \cos \beta + \sin \beta}$$

$$g \sin \beta$$

Задача

N1

$$S^2 = S_1^2 + S_2^2$$

$$S_1 = x(1 - \cos \alpha) = \frac{a_2 t^2}{2} (1 - \cos \alpha)$$

3)

(S_1 - гориз. перем. шара влево)
(x - перем. клина (a_2 - уск. клина))

$$S_2 = x \sin \alpha = \frac{a_2 t^2}{2} \sin \alpha$$

S_2 - верт. перем. шара вниз

$$\frac{a t^2}{2} = \frac{a_2 t^2}{2} \sqrt{(1 - \cos \alpha)^2 + \sin^2 \alpha}$$

$$a = a_2 \sqrt{2 - 2 \cos \alpha}$$

$$m a \cos \beta = T \cos \alpha$$

$$M a_2 = T \sin \alpha$$

$$\frac{M a_2}{m a \cos \beta} = \operatorname{tg} \alpha$$

$$\frac{M a_2}{m a_2 \sqrt{2 - 2 \cos \alpha} \cos \beta} = \operatorname{tg} \alpha$$

$$\frac{M}{m} = \operatorname{tg} \alpha \cos \beta \sqrt{2 - 2 \cos \alpha} = \frac{4 \cdot 5 \cdot 1}{5 \cdot 3 \cdot \sqrt{5}} \sqrt{2 - \frac{6}{5}} =$$

$$= \frac{4 \sqrt{5}}{15 \sqrt{5}} = \frac{8}{15}$$

$$\frac{M}{m} = \frac{8}{15}$$

$$\frac{m}{M} = \frac{15}{8}$$

$$2) a_2 = \frac{a}{\sqrt{2 - 2 \cos \alpha}} = \frac{g}{(\operatorname{tg} \alpha \cos \beta + \sin \beta) \sqrt{2 - 2 \cos \alpha}} = \frac{g}{\left(\frac{4}{3} \sqrt{5} + \frac{2}{\sqrt{5}}\right) \sqrt{5}}$$

$$a_2 = \frac{g}{\frac{8}{15} + \frac{4}{5}} = \frac{g \cdot 15}{20} = \frac{3g}{4}$$

1,875

21200737 (U342273 M1269938)

Ответ: $\operatorname{tg} \beta = 2$; $\frac{3}{4}g$; $\frac{8}{15}$; $\sqrt{\frac{10H}{3g}}$

(2)

N2

Термодинамика

Физика

$$C(T) = 2R \frac{T}{T_0} \quad i=5$$

$$Q'(T) = C(T) \dot{T} = 2R \frac{T}{T_0} \dot{T}$$

$$Q(T) = \int_{T_0}^{\frac{5}{6}T_0} 2R \frac{T}{T_0} dT = \int_{T_0}^{\frac{5}{6}T_0} \frac{2R \left(\left(\frac{5}{6}T_0 \right)^2 - T_0^2 \right)}{2T_0} = R \frac{25-36}{36} T_0 =$$

$$= -\frac{11}{36} R T_0$$

так обратн $-Q = \frac{11}{36} R T_0$

$$Q = A + \Delta U$$

$$Q = \sqrt{R} \frac{T_1^2 - T_0^2}{T_0}$$

$$\Delta U = \frac{5}{2} \sqrt{R} (T_1 - T_0)$$

$$\frac{\sqrt{R} (T_1 - T_0) (T_1 + T_0)}{T_0} = A + \frac{5}{2} \sqrt{R} (T_1 - T_0)$$

$$\sqrt{R} (T_1 - T_0) \left(\frac{T_1 + T_0}{T_0} - \frac{5}{2} \right) = A$$

$$\frac{A}{\sqrt{R}} = (T_1 - T_0) \left(\frac{2T_1 - 3T_0}{2T_0} \right) = \frac{2T_1^2 - 5T_1 T_0 + 3T_0^2}{2T_0}$$

Минимум работы достигается в минимуме
числителя $T_1 = \frac{+3T_0}{4}$ ($\frac{-b}{2a}$ параболы с ветвями вверх)

Отв.: $\frac{3T_0}{4}$

$$A_{\min} = \sqrt{R} \cdot \frac{\frac{2 \cdot 9T_0^2}{16} - 3T_0 \frac{3T_0}{4} + T_0^2}{2T_0} = \sqrt{R} \left(\frac{9}{16} T_0 - \frac{9T_0}{8} + \frac{T_0}{2} \right) =$$

$$= -\frac{\sqrt{R} T_0}{16}$$

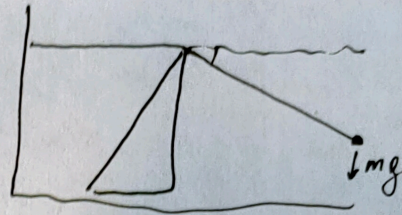
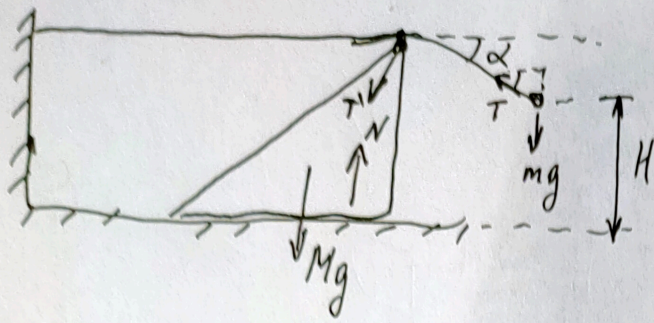
Отв.: $-\frac{\sqrt{R} T_0}{16}$

(минимальная по модулю работа -0 , достигается при $\frac{T_0}{2}$)

Отв.: $\frac{11}{36} R T_0$; $\frac{3T_0}{4}$; $-\frac{\sqrt{R} T_0}{16}$

3

N1

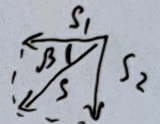


$a \uparrow \uparrow S$

$-x \cos \alpha - x \cos \alpha$

$S_1 = x + x \cos \alpha - x \cos \alpha = x(1 - \cos \alpha)$

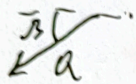
$S_2 = 2x \sin \alpha - x \sin \alpha = x \sin \alpha$



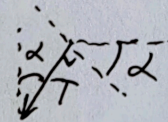
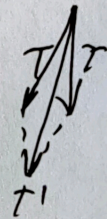
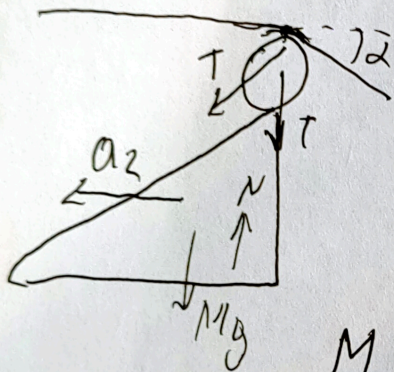
$S^2 = S_1^2 + S_2^2$

$\text{tg } \beta = \frac{S_2}{S_1} = \frac{\sin \alpha}{1 - \cos \alpha} = \frac{\frac{4}{5}}{1 - \frac{3}{5}} = \frac{4}{5} : \frac{2}{5} = 2$

1)

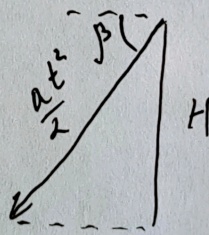
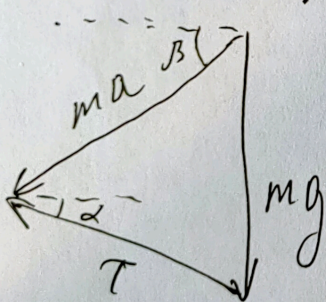


ответ: $\beta = \text{arctg } 2 = 0,79 \text{ рад}$



$M a_2 = T \sin \alpha$

где масса



$\frac{a t^2}{2} \sin \beta = H$

4)

$$\begin{cases} T \sin \alpha + m a \sin \beta = m g \\ T \cos \alpha = m a \cos \beta \end{cases}$$

$$\begin{cases} T \sin \alpha = m(g - a \sin \beta) \\ T \cos \alpha = m a \cos \beta \end{cases}$$

$$\text{tg } \alpha = \frac{g - a \sin \beta}{a \cos \beta}$$

$t = \sqrt{\frac{H \cdot 2}{a \cdot \sin \beta}} = \sqrt{\frac{2H}{g \cdot \text{tg } \beta + 1}}$

$t = \sqrt{\frac{2H \cdot 5}{g \cdot 3}} = \sqrt{\frac{20H}{3g}}$

$212007 \text{ g} + \dots$

$a = \frac{g}{\text{tg } \alpha \cos \beta + \sin \beta}$

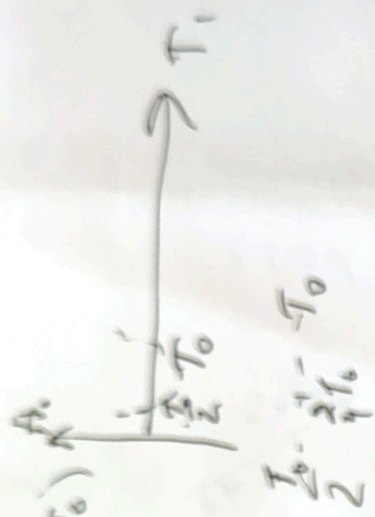
1

(v)

$$Q = \int c(T) v dt$$

$$Q = \int \frac{2RT}{T_0} dT = \frac{2RT^2}{2T_0} \Big|_{T_0}^{\frac{5}{6}T_0}$$

$$\frac{R}{T_0} T_0^2 \left(\left(\frac{5}{6} \right)^2 - 1 \right) = \frac{25-36}{36}$$



$$(T_1 - T_0)(2T_1 - T_0) = \frac{T_0 - 2T_0}{2} = \frac{-T_0}{2}$$

$$Q = A + \Delta U$$

$$vR \frac{T_1^2 - T_0^2}{T_0} = A + vR(T_1 - T_0)$$

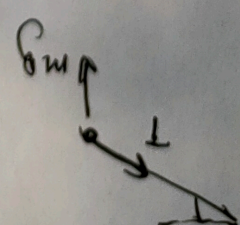
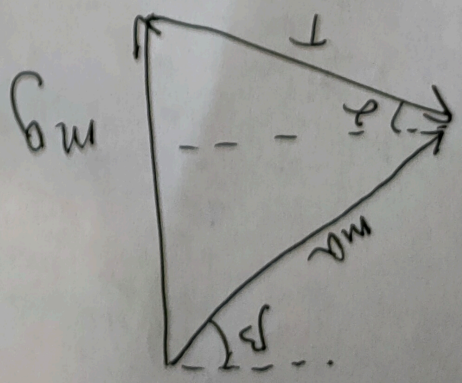
$$vR \left(\frac{2T_1 T_0 - 3T_0^2}{2T_0} \right) = \frac{9 - 18 + 8}{16}$$

$$(T_1 - T_0) \frac{2T_1 - T_0}{2T_0}$$

$$\frac{m a}{M a z} = \frac{c v \beta}{c v \beta}$$

$$M a z = T \sin \alpha$$

$$m a \cos \beta = T \cos \alpha$$



Часть 2

Олимпиада: **Физика, 11 класс (2 часть)**

Шифр: **21200737**

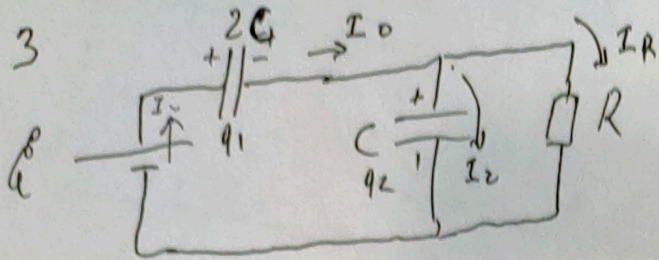
ID профиля: **342273**

Вариант 1

Устройство

Грузика

№ 3



$$\frac{q_2}{C} = I_R R$$

$$\mathcal{E} = \frac{q_1}{2C} + \frac{q_2}{C} = \text{const}$$

$$\mathcal{E}' = 0 = \frac{I_1}{2C} + \frac{I_2}{C}$$

$$I_1 = I_0$$

$$I_2 = I_0 - I_R$$

$$\frac{I_0}{2C} = \frac{I_R - I_0}{C}$$

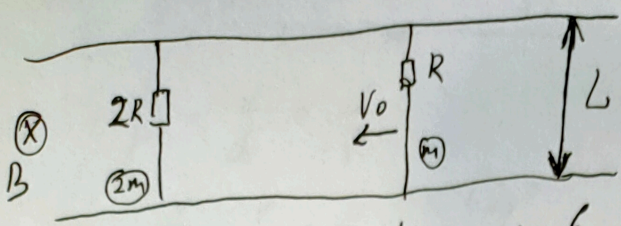
$$I_R = \frac{3}{2} I_0$$

Ответ: $\frac{2\mathcal{E}}{3R}$, $\frac{2C\mathcal{E}^2}{3}$, $\frac{3}{2} I_0$

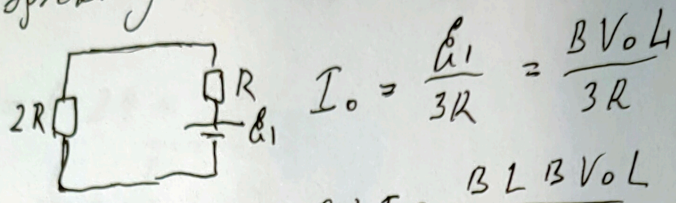
№ 4

Задача

Физика



По закону Холла: $\mathcal{E}_1 = B V_0 L$



$$I_0 = \frac{\mathcal{E}_1}{3R} = \frac{B V_0 L}{3R}$$

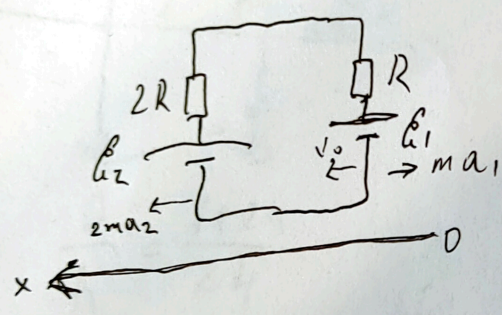
$$2m a = F_A = B L I = \frac{B^2 L^2 V_0 L}{3R}$$

$$a = \frac{B^2 L^2 V_0}{6mR}$$

(Сила ампера всегда является тормозной силой ~~и т.д.~~
Значит в конце $F_A = 0$ (тока нет))

$$2m a_{2x} = B L I(t) = \frac{B L (\mathcal{E}_1 - \mathcal{E}_2)}{3R} = \frac{B^2 L^2 (V_{1x} - V_{2x})}{3R}$$

$$m a_{1x} = \frac{B^2 L^2 (V_{1x} - V_{2x})}{3R}$$



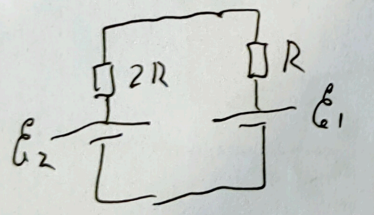
(интегрируем по dt)

$$2m V_{2x} = \frac{B^2 L^2}{3R} (s - s_0)$$

$$m (V_{1x} - V_0) = \frac{B^2 L^2}{3R} (s - s_0)$$

($s - s_0$ — изменение расстояния между рельсами)

уст. режим:



$$\mathcal{E}_1 = \mathcal{E}_2 \quad I = 0$$

$$V_1 = V_2$$

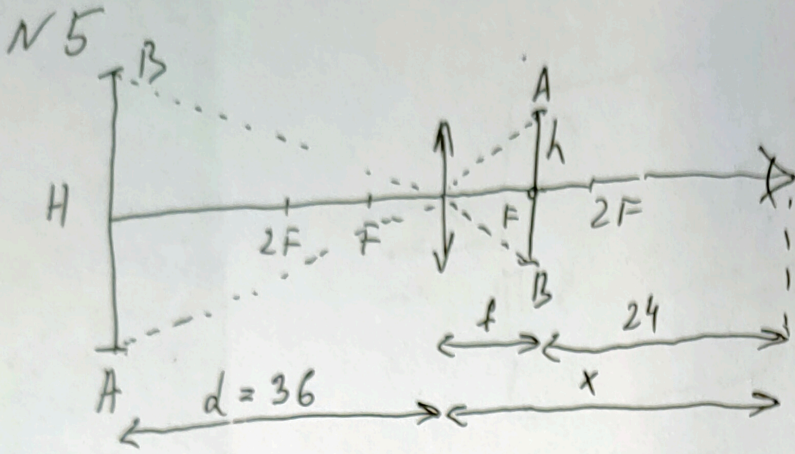
$$2V_{2x} = V_{1x} - V_0$$

$$V_0 = V_{1x} - 2V_{2x} = -V_{1x}$$

По условию $V_1 = V_2 = V_0$

$$s = \frac{-2m V_0 \cdot 3R}{B^2 L^2} + s_0$$

Ответ: $\frac{B^2 L^2 V_0}{6mR}$; V_0 ; $-\frac{6m V_0 R}{B^2 L^2} + s_0$



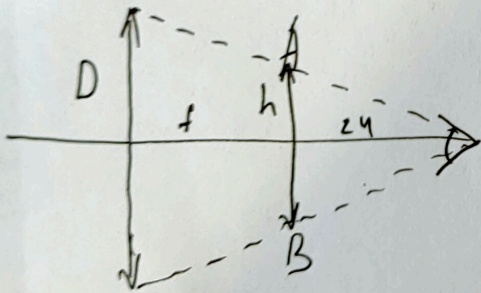
$$\frac{1}{F} = \frac{1}{d} + \frac{1}{f}$$

$$\frac{1}{f} = -\frac{1}{36} + \frac{1}{9} = \frac{4-1}{36} = \frac{3}{36} = \frac{1}{12} \quad f = 12 \text{ см}$$

$$x = f + 24 = 36 \text{ см}$$

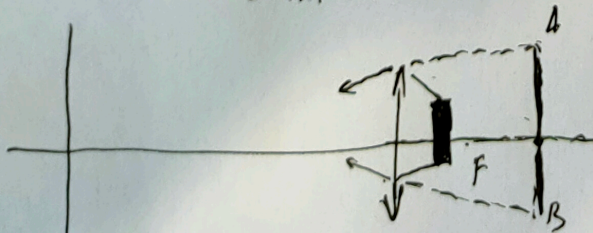
$$\Gamma = \frac{h}{H} = \frac{f}{d} = \frac{12}{36} = \frac{1}{3}$$

$$h = \frac{H}{3}$$



$$\frac{D}{h} = \frac{f+24}{24}$$

$$D_{\min} = \frac{H}{3} \cdot \frac{f+24}{24} = \frac{9}{3} \cdot \frac{12+24}{24} = \frac{36 \cdot 3}{24} = \frac{36}{2} = 18 \text{ см}$$



Если поместить экран справа от линзы перед фокусом его мнимое изобр. наложится на изобр. картины.

$$\frac{1}{F} = \frac{1}{d_1} - \frac{1}{f}$$

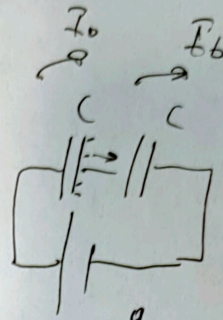
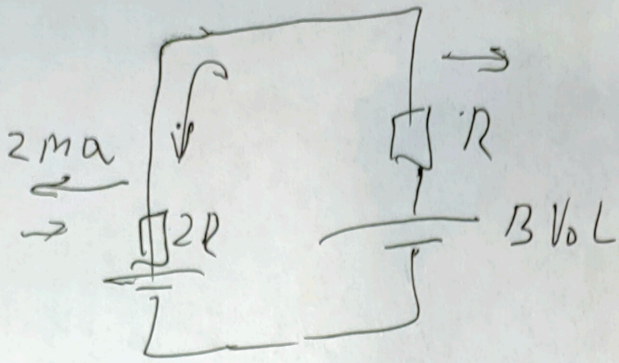
$$\frac{1}{9} = \frac{1}{d_1} - \frac{1}{12}$$

$$\frac{1}{d_1} = \frac{7}{36} \quad d_1 = \frac{36}{7} = 5\frac{1}{7} \text{ см}$$

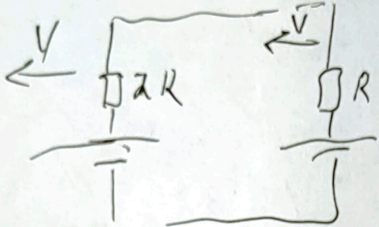
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от картины 4,1 см; от изобр. — 6,85 см

Ответ: 36 см; 18 см; 5,14 см



$$\frac{q}{C} + \frac{q}{C} = \mathcal{E}$$



$$U = \frac{q}{2C}$$

$$\frac{3A}{2} + \dots \Rightarrow Q_1 = CU_2$$

$$U_2 = I_2 R$$

$$U_2 = (q - q_1) R$$

$$q = 2CU_1$$

$$U_2 = (2CU_1 - CU_2) R$$

$$\frac{U_2}{CR} = 2U_1 - U_2$$

$$-3U_2$$

$$U_2 = -3CRU_2$$

$$U_1 + U_2 = 0$$

$$I_R R = \frac{q_2}{C}$$

$$\frac{q_2}{C} = I_R R$$

$$\mathcal{E} = \frac{q_1}{2C} + \frac{q_2}{C}$$

$$I_0 = I_2 + I_R$$

$$\mathcal{E} = 2CI_0 + \frac{q_2}{C} = R I_R$$

$$\mathcal{E} = \frac{I_1}{2C} + \frac{I_2}{C} = 0$$

$$\mathcal{E} = \frac{q_0}{2C} + \frac{q_2}{C} = I_0 - I_R$$

$$\frac{1}{F} = \frac{1}{d} + \frac{1}{f}$$

$$= \frac{q_0}{2C} + I_R R = I_R R$$

$$\frac{1}{g} = \frac{1}{d} - \frac{1}{12}$$

$$q_1 = 2CU_1$$

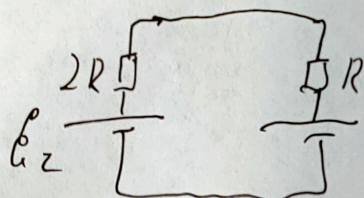
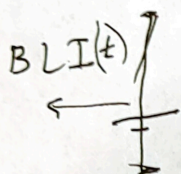
$$I_0 - I_R = I_R R C$$

$$\frac{1}{d} = \frac{7}{36} \quad d = \frac{36}{7}$$

$$q_2 = CU_2$$

$$U_1 + U_2 = \mathcal{E} \quad \mathcal{E} = \Phi' = B S' = B (a_0 - v_0 t) L =$$

$$\mathcal{E} = B L v_0$$



$$\Phi = B(S_0 - S) L$$

$$\mathcal{E}_1 = B L v_1(t)$$

$$2m a_{1x} = B^2 L^2 \frac{v_{1x} + v_{2x}}{3R}$$

$$\mathcal{E}_2 = B L v_2(t)$$

$$m a_{2x} = B^2 L^2 \frac{v_{1x} + v_{2x}}{3R}$$

$$I = \frac{B L (v_1(t) - v_2(t))}{3R}$$

$$2m(v_{1x} - v_0) = B^2 L^2 \frac{\Delta S}{3R}$$

$$m v_{2x} = B^2 L^2 \frac{\Delta S}{3R}$$

$$\leftarrow 2m a_2 = \frac{B^2 L^2 (v_1(t) - v_2(t))}{3R}$$

$$2v_{1x} - 2v_0 = v_{2x}$$

$$2v_{1x} - v_{2x} = 2v_0$$

$$\rightarrow m a_1 = \frac{B^2 L^2 (v_1(t) - v_2(t))}{3R}$$

$$\frac{1}{g} = \frac{1}{d} = \frac{1}{36}$$

$$\frac{1}{F} = \frac{2}{F}$$

$$\frac{1}{d} = \frac{5}{36}$$

$$2m v_2 = \frac{B^2 L^2}{3R} (S_1 - S_2)$$

$$d = 36/5$$

$$m(v_1 - v_0) = \frac{B^2 L^2}{3R} (S_1 - S_2)$$

$$\frac{1}{F} = -\frac{1}{F} + \frac{1}{F}$$

$$\frac{1}{g} = \frac{1}{d} + \frac{1}{36}$$

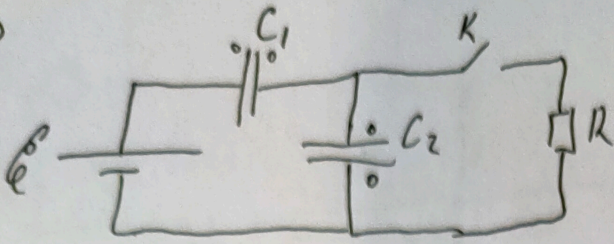
$$m v_2 = m v_1 - m v_0$$

$$v_0 = v_1 - v_2$$

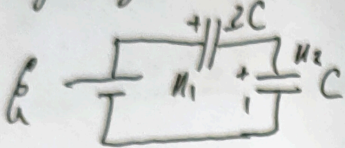
$$\frac{1}{g} = -\frac{1}{d} + \frac{1}{12}$$

$$\frac{1}{d} = \frac{1}{12} - \frac{1}{8} = \frac{3-4}{4 \cdot 3 \cdot 3}$$

№3



до замыкания ключа:



$$\varepsilon = U_1 + U_2 = \frac{q_1}{C_1} + \frac{q_2}{C_2}$$

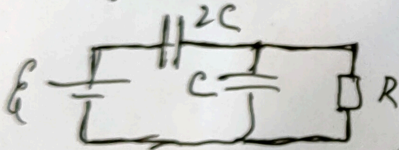
по ЗСЗ: $q_1 = q_2 = q$
 $(0 = -q_1 + q_2)$

$$\varepsilon = \frac{q}{2C} + \frac{q}{C} = \frac{3q}{2C}$$

$$U_1 = \frac{q}{2C} = \frac{\varepsilon}{3}$$

$$U_2 = \frac{q}{C} = \frac{2}{3}\varepsilon$$

сразу после \times K :

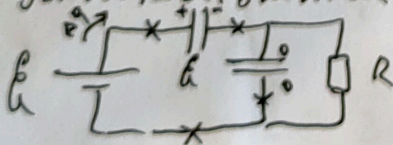


$$U_R = U_2 = \frac{2\varepsilon}{3}$$

$$I \cdot R = \frac{2\varepsilon}{3}$$

$$I_0 = \frac{2\varepsilon}{3R}$$

Установившийся режим (ток через конденс. не идет)



Очевидно, через резис. R ток тоже идти не сможет.

$$0 \cdot R = U_R' = U_2' = 0$$

$$U_1' = \varepsilon$$

$$A_{\text{э}} = \Delta U + Q$$

$$\Delta U = \frac{2C\varepsilon^2}{2} - \left(\frac{2C\varepsilon^2}{2 \cdot 3} + \frac{C \left(\frac{2}{3}\varepsilon \right)^2}{2} \right) = C\varepsilon^2 - \frac{C\varepsilon^2}{9} - \frac{2}{9}C\varepsilon^2$$

$$\Delta U = \frac{2}{3}C\varepsilon^2$$

$$A_{\text{э}} = \varepsilon \cdot q = \varepsilon \left(2C\varepsilon - \frac{2C\varepsilon}{3} \right) = \frac{4}{3}C\varepsilon^2$$

$$Q = -\frac{2}{3}C\varepsilon^2 + \frac{4}{3}C\varepsilon^2 = \frac{2}{3}C\varepsilon^2$$