

# Часть 1

Олимпиада: **Физика, 11 класс (1 часть)**

Шифр: **21203393**

ID профиля: **66081**

Вариант 1

Механика  
№2

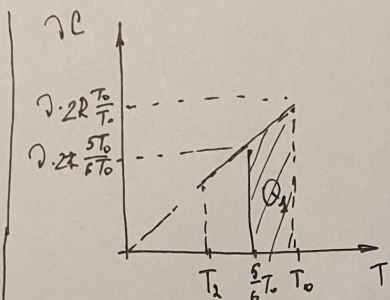
Задача

$\frac{\partial}{\partial T_0}$   
 $C(T) = 2R \frac{T}{T_0}$

1)  $Q_1$

2)  $T_2$

3)  $A_{min}$



1)  $\delta Q: \partial_T C(T) = -3R \Rightarrow \delta Q_1 = -\delta Q = +3R \delta T$

$Q_1 = 3R \delta T$

$Q_1 = \frac{2R \left( \frac{T_0}{T_0} + \frac{5T_0}{6T_0} \right)}{2} \cdot \left( T_0 - \frac{5}{6} T_0 \right)$

$Q_1 = \frac{11 \cdot 2R}{6} \cdot \frac{1}{6} T_0 = \frac{11 \cdot 2R T_0}{36}$

2) Степной закон периодичности

$Q: \Delta U + A$

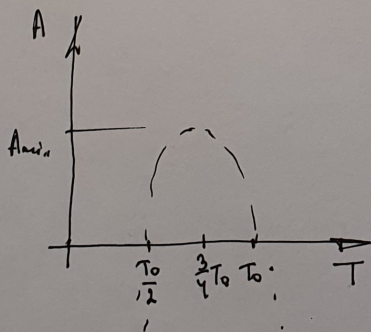
$\frac{1}{2} (T_2 - T_0) \cdot 2R \left( \frac{T_0}{T_0} + \frac{T_2}{T_0} \right) = \frac{3}{2} 2R (T_2 - T_0) + A$

$2R (T_2 - T_0) \left( 1 + \frac{T_2}{T_0} \right) - 3R (T_2 - T_0) = A$

$2R (T_2 - T_0) \left( 1 + \frac{T_2}{T_0} - 1.5 \right) = A$

$2R (T_2 - T_0) \left( \frac{T_2}{T_0} - 0.5 \right) = A$

$\frac{2R (T_2 - T_0) (2T_2 - T_0)}{2T_0} = \frac{2R (2T_2^2 - 3T_2 T_0 + T_0^2)}{2T_0} = A$



$T_2 - T_0 < 0 \Rightarrow$  в вершине  $A = A_{min}$

$T_2 = \frac{+3T_0}{4} = \frac{3}{4} T_0$

3)  $A_{min} = A \left( \frac{3}{4} T_0 \right) = \frac{2R \left( \frac{3}{4} T_0 - T_0 \right) \left( \frac{3}{2} T_0 - T_0 \right)}{2T_0}$

$A_{min} = \frac{2R \left( -\frac{T_0}{4} \right) \left( \frac{T_0}{2} \right)}{2T_0} = -\frac{2R T_0}{16}$

Ответ: 1)  $Q_1 = \frac{11 \cdot 2R T_0}{36}$  2)  $T_2 = \frac{3}{4} T_0$  3)  $A_{min} = -\frac{2R T_0}{16}$

1



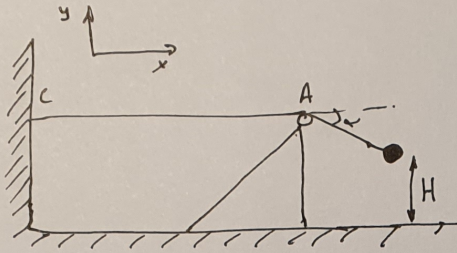
Местовик  
№1

Дано:

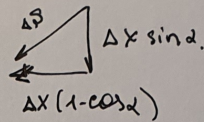
$\cos \alpha = \frac{3}{5}$   
 $(\sin \alpha = \frac{4}{5})$

H

- 1)  $\beta$
- 2)  $a_{\text{кн}}$
- 3)  $\frac{m}{M}$
- 4) t

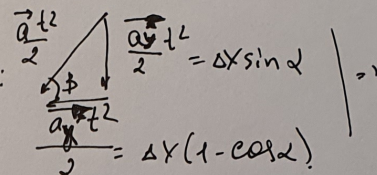


1) Пусть кин. смещение на  $\Delta x$ , тогда шарик сместился на  $\Delta x \sin \alpha$  по оси  $y$  и на  $\Delta x \cos \alpha$  по  $x$ , т.е.



Учитывая, что  $v(0) = 0 \Rightarrow$

в треугольнике перемещений:



$$\Rightarrow \operatorname{tg} \beta = \frac{a_y t^2 / 2}{a_x t^2 / 2} = \frac{\Delta x \sin \alpha}{\Delta x (1 - \cos \alpha)} = \frac{\sin \alpha}{1 - \cos \alpha} = \frac{4/5}{1 - 3/5} = \frac{4/5}{2/5} = 2.$$

$\sin \beta = \frac{4}{2\sqrt{5}} = \frac{2}{\sqrt{5}}$   
 $\cos \beta = \frac{2}{2\sqrt{5}} = \frac{1}{\sqrt{5}}$

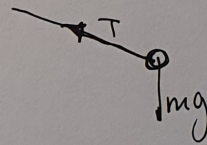
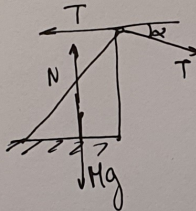
2) II. З.И. для кн.

X:  $T - T \cos \alpha = M a_{\text{кн}}$

II ЗИ для шара:

X:  $-T \cos \alpha = m a_{\text{ш.ш}}$

$a_{\text{ш.ш}} = a_{\text{кн}} (1 - \cos \alpha)$   
(из кин. связей перемещений)



$$\begin{cases} T(1 - \cos \alpha) = M a_{\text{кн}} \\ T \cos \alpha = m a_{\text{кн}} (1 - \cos \alpha) \end{cases} \Rightarrow \frac{T(1 - \cos \alpha)}{T \cos \alpha} = \frac{M a_{\text{кн}}}{m a_{\text{кн}} (1 - \cos \alpha)} \Rightarrow \frac{1 - \cos \alpha}{\cos \alpha} = \frac{M}{m(1 - \cos \alpha)}$$

$$\frac{(1 - \cos \alpha)^2}{\cos \alpha} = \frac{M}{m} \Rightarrow \frac{4}{15} \cdot 5 = \frac{4}{15} \frac{M}{m} \Rightarrow m = \frac{15M}{4}$$

3) ЗСЭ:  $mgh = \frac{(m+M)U^2}{2} \Rightarrow \frac{15M}{4} g \cdot \frac{19H}{4} \cdot \frac{1}{2} \Rightarrow U^2 = \frac{30gH}{19}$  (1)

$H = \frac{a_y t^2}{2} \Rightarrow 2H = a_{\text{кн}} \cdot \sin \alpha t^2 \Rightarrow a_{\text{кн}} t^2 = \frac{2H}{\sin \alpha}$  (2)

$v = a_{\text{кн}} t \Rightarrow v^2 = a_{\text{кн}}^2 t^2 \leftarrow (1); (2)$

$a_{\text{кн}} \cdot \frac{2H}{\sin \alpha} = \frac{30gH}{19} \Rightarrow a_{\text{кн}} \cdot \frac{15g}{19} \cdot \sin \alpha = \frac{15g}{19} \cdot \frac{4}{5} = \frac{12}{19} g$

4)  $H = \frac{a_{\text{кн}} \sin^2 t^2}{2} \Rightarrow \sqrt{\frac{2H}{a_{\text{кн}} \sin^2}} = t = \sqrt{\frac{2H}{\frac{12}{19} \cdot \frac{4}{5}}} \Rightarrow t = \sqrt{\frac{95H}{24g}}$

Ответ:  $\operatorname{tg} \beta = 2$ ;  $a_{\text{кн}} = \frac{12}{19} g$ ;  $\frac{m}{M} = \frac{15}{4}$ ;  $t = \sqrt{\frac{95H}{24g}}$

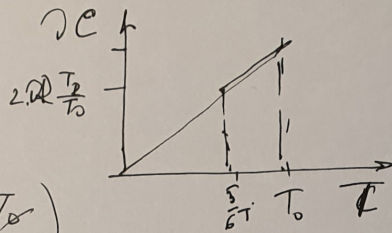
2



# Чепнабух

$$C(T) = 2R \frac{T}{T_0}$$

0



$$Q = \frac{1}{2} \cdot \frac{T_0}{6} \left( \frac{2R T_0}{T_0} + \frac{2R \cdot 5 T_0}{T_0} \right)$$

$$Q = \frac{Q T_0}{T_0} \left( 2R + \frac{5R}{3} \right) = \frac{11 R T_0}{3}$$

$$\frac{2R(T_0 + \frac{5}{6} T_0)}{2} \cdot \frac{1}{6}$$

$$Q = \frac{1}{2} \Delta T \cdot \frac{2R}{T_0} (T_1 + T_2) = \frac{3}{2} R (T_2 - T_1) + A.$$

$$\left( \frac{2R}{T_0} (T_1 + T_2) - \frac{3}{2} R \right) (T_2 - T_1) = A.$$

$$2R \left( \frac{2T_1 + 2T_2 - 3T_0}{2T_0} \right) (T_2 - T_1) = A.$$

$$T_1 + T_2 = \frac{3}{2} T_0 \quad \left( T_2 - T_0 \right) \left( \frac{2T_2 - T_0}{2T_0} \right)$$

$$T_2 \cdot \frac{1}{2} T_0 \quad \left( 2T_2^2 - 2T_2 T_0 - T_2 T_0 + T_0^2 \right)$$

$$Q = \frac{1}{2} \Delta T (T_2 - T_0) \cdot 2R \left( \frac{T_2}{T_0} + \frac{T_0}{T_0} \right) = \frac{2R(T_2 - T_0)(T_2 + T_0)}{T_0}$$

$$Q = \frac{3}{2} R (T_2 - T_0) + A$$

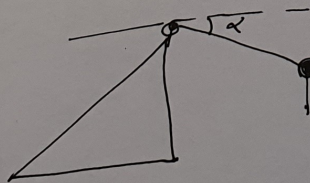
$$2R (T_2 - T_0) \left( \frac{2T_2 + 2T_0 - 3T_0}{2T_0} \right) \neq A$$

$$\Rightarrow \frac{2R (T_2 + T_0) (2T_2 - T_0)}{2T_0} \neq A.$$

$$2R \left( \frac{-T_0}{4} \right) \left( \frac{3T_0}{2} - T_0 \right)$$

$$\frac{2R \left( \frac{-T_0}{4} + \frac{T_0}{2} \right)}{2T_0} = A.$$

$$2R \quad - \frac{3T_0}{4} -$$



$$mgh = \frac{m(v_{\text{max}})^2}{2} = \frac{(M+m)U^2}{2}$$

$$\frac{15}{4} M = \frac{19}{4} M \frac{U^2}{2}$$

$$\frac{30gh}{19} = U^2$$

$$U^2 = a^2 t^2 = \frac{30gh}{19} = a \cdot 2t \Rightarrow a = \frac{19}{30} g.$$



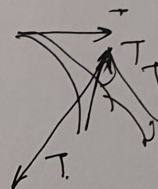
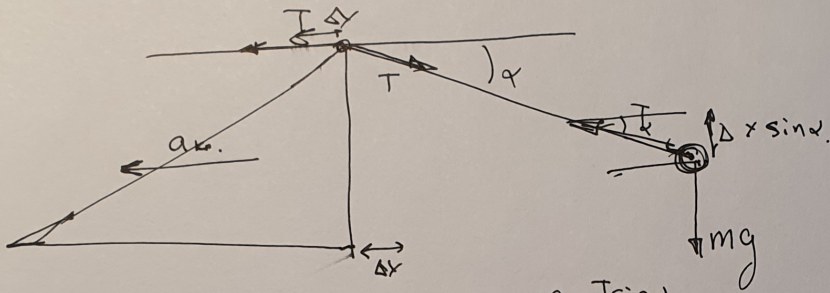
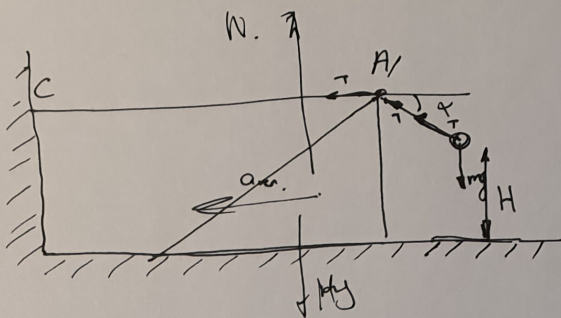
# Упруобук

β = const.

$$\text{height} = \frac{m \cdot 0.54^2}{2}$$

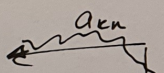
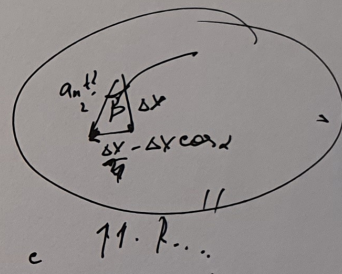
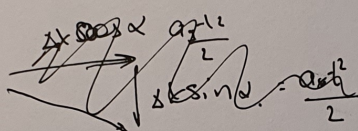
$$\frac{a \cdot l^2}{2} =$$

$$a_y = \text{const.}$$



$$\alpha: \text{const.} = 1$$

$$a_y = \frac{mg - T \sin \alpha}{m} \quad a_x =$$



Мапуа норааесен гбер но оуп с  
нпу эмбу а<sub>y</sub> = const.

$$M \cdot a_{cn} = T - T \cos \alpha$$

$$T \cos \alpha = m a_{cn} (\text{to be corrected}) (1 - \cos \alpha)$$

$$T(1 - \cos \alpha) = M a_{cn}$$

$$\Rightarrow \frac{T \cos \alpha}{1 - \cos \alpha} = M a_{cn}$$

$$T \cdot \frac{1}{1 - \cos \alpha} = M a_{cn}$$

$$\frac{M}{m} : (1 - \cos \alpha)^2 = \frac{4}{25}$$

$$\frac{4}{5} \cdot \frac{25}{4} = \frac{m}{M} = 5$$

$$m = \frac{M \cos \alpha}{(1 - \cos \alpha)}$$

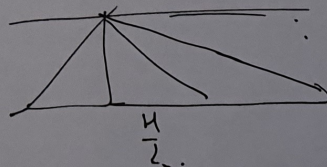
$$T - T \cos \alpha = T(1 - \cos \alpha) = M \cdot a_{cn}$$

$$T \cos \alpha = \frac{M \cos \alpha}{(1 - \cos \alpha)^2}$$

$$H = \frac{a_y t^2}{2}$$

$$\sqrt{\frac{2H}{a_y}} = t \quad \sqrt{\frac{2H}{a_{cn} \cdot \frac{4}{5}}} = t = \sqrt{\frac{15H}{\frac{1}{2} a_{cn}}} = t$$

$$\frac{H}{2} = \frac{a_{cn}(1 - \cos \alpha)}{2} t^2 \quad \frac{5H}{2}$$





# Часть 2

Олимпиада: **Физика, 11 класс (2 часть)**

Шифр: **21203393**

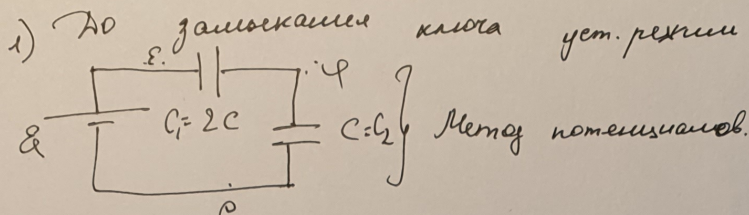
ID профиля: **66081**

Вариант 1



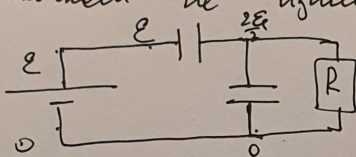
Дано  
 $C_2 = C$   
 $C_1 = 2C$   
 $\mathcal{E}, R$

- 1)  $I$   
 2)  $Q$   
 3)  $I_1$



$$2C(\mathcal{E} - \varphi) = C\varphi \Rightarrow \varphi = \frac{2\mathcal{E}}{3}$$

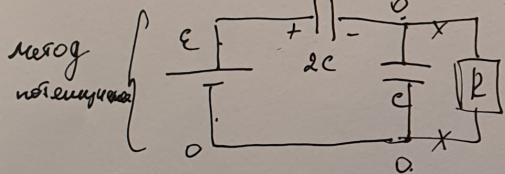
2) После замыкания ключа напряжение на конденсаторах скакнет и уменьшится  $\Rightarrow$



$$I = \frac{2\mathcal{E}}{3R}$$

$$W(0) = \frac{2C \cdot \left(\frac{\mathcal{E}}{3}\right)^2}{2} + \frac{C \left(\frac{2\mathcal{E}}{3}\right)^2}{2} = \frac{C}{2} \left( \frac{2\mathcal{E}^2}{9} + \frac{4\mathcal{E}^2}{9} \right) = \frac{6\mathcal{E}^2}{3}$$

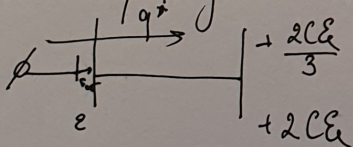
3) Установившийся режим при замкнутом ключе: ток через конденсаторы не идет  $\Rightarrow$



$\Rightarrow$  и через резистор тоже нет тока

$$W(\text{уст}) = \frac{2C \cdot \mathcal{E}^2}{2} = C\mathcal{E}^2$$

4) Переходный процесс от замыкания ключа до уст. режима

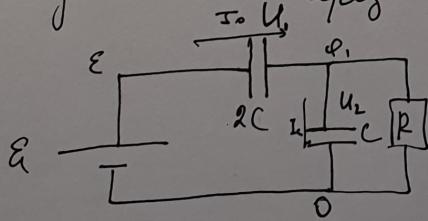


$$q^* = 2C\mathcal{E} - \frac{2C\mathcal{E}}{3} = \frac{4CE}{3}$$

$$\Delta\delta = \frac{4CE^2}{3}$$

$$\text{ЗЭЭ: } \Delta\delta = \Delta W + Q \Rightarrow \frac{4CE^2}{3} = CE^2 - \frac{CE^2}{3} + Q \Rightarrow \frac{5CE^2}{3} - CE^2 = Q \Rightarrow Q = \frac{2CE^2}{3}$$

5) Когда ток через  $C_1 = 0$



$$I_0 = I_C + I_1$$

$$I_0 \cdot C = \dot{q}_1 = 2C\dot{U}_1 \Rightarrow \frac{I_0}{2C} = \dot{U}_1$$

$$U_1 = -U_2 \Rightarrow \frac{I_0}{2C} \cdot C = I_C \Rightarrow \frac{I_0}{2} \Rightarrow I_0 = \frac{I_0}{2} + I_1 \Rightarrow I_1 = \frac{I_0}{2}$$

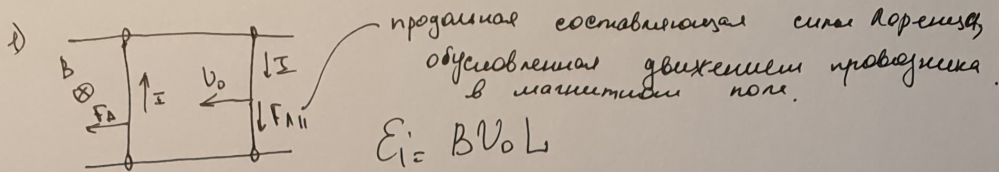
Ответ:  $I = \frac{2\mathcal{E}}{3R}$      $Q = \frac{2CE^2}{3}$      $I_1 = \frac{I_0}{2}$

1



№4

Дано  
 $v_0, m, L, R, B$



- 1)  $a$
- 2)  $u_1, u_2$
- 3)  $S_1, S_2$

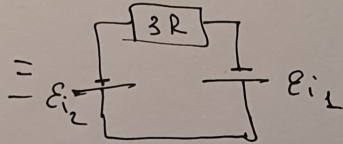
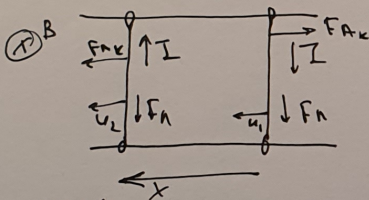
2)  $I = \frac{\mathcal{E}_i}{3R} = \frac{BLv_0}{3R}$

II З.И. где второй перемычки

4)  $F_A = 2ma$

$BI L = 2ma \Rightarrow a = \frac{BIL}{2m} = \frac{B^2 L^2 v_0}{2m \cdot 3R} = \frac{B^2 L^2 v_0}{6mR}$

2) Через предельно большой промежуток времени.



Спустя долгое время ускорение рамок = 0  $\Rightarrow F_A = 0$   
 $\Rightarrow I = 0 \Rightarrow \mathcal{E}_{i2} = \mathcal{E}_{i1} \Rightarrow$

$BLu_2 L = BLu_1 L \Rightarrow u_2 = u_1 = u$

$3mu = mv_0 = 2mu_2 + mu_1 \Rightarrow mv_0 = 3mu \Rightarrow u = \frac{v_0}{3} = u_1 = u_2$

3)  $\mathcal{E}_{i \text{ экв}} = \mathcal{E}_{i1} - \mathcal{E}_{i2}(t) = BL(v_1(t) - v_2(t)) \Rightarrow I(t) = \frac{BL(v_1(t) - v_2(t))}{3R}$

II З.И. где первой перемычки в предельно большой момент времени

$x: -F_A(t) = max \Rightarrow$

$-\frac{B^2 L^2}{3R} (v_1(t) - v_2(t)) = m \frac{\Delta v_x}{\Delta t} \cdot \Delta t$  где  $v(t) = \frac{\Delta S}{\Delta t}$

$-\frac{B^2 L^2}{3R} (S_1 - \Delta S_2) = m \Delta v$ , просуммируем за всё время передвижения.

$-\frac{B^2 L^2}{3R} (S_1 - S_2) = m \left( \frac{v_0}{3} - v_0 \right) \Rightarrow \frac{B^2 L^2}{3R} (S_1 - S_2) = \frac{2mv_0}{3}$

$S_1 - S_2 = \frac{2mv_0 R}{B^2 L^2}$

4) т.к.  $S_1 - S_2 > 0 \Rightarrow$  первая перемычка приблизится ко второй  $\Rightarrow$

$\Rightarrow S_k = S_0 - (S_1 - S_2) = S_0 - \frac{2mv_0 R}{B^2 L^2}$

Ответ: 1)  $a = \frac{B^2 L^2 v_0}{6mR}$  2)  $u_1 = \frac{v_0}{3}$   $u_2 = \frac{v_0}{3}$  3)  $S_k = S_0 - \frac{2mv_0 R}{B^2 L^2}$

2



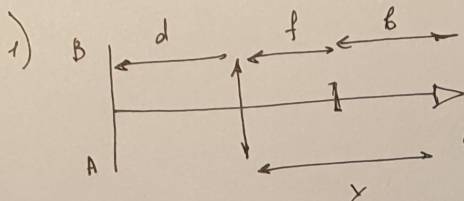
Дано

$F = 9 \text{ см}$

$H = 9 \text{ см}$

$d = 36 \text{ см}$

$b = 24 \text{ см}$



$\frac{1}{d} + \frac{1}{f} = \frac{1}{F}$

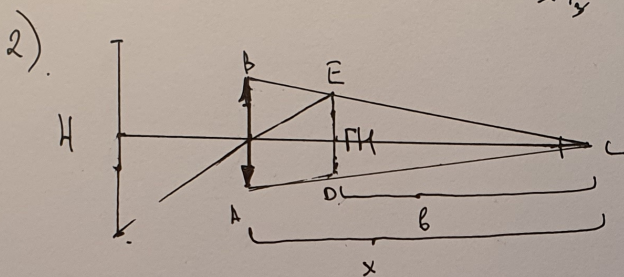
Для линзы картина - действительной предмет на  $d > F \Rightarrow$  изображение действительное

$f = \frac{dF}{d-F}$

$\Gamma = \frac{F}{d-F} = \frac{1}{3}$

$x = b + f = b + \frac{dF}{d-F} = 24 + \frac{36 \cdot 9}{24-9} = 36 \text{ см}$

- 1) X
- 2) D<sub>н</sub>
- 3) Где экран! C



Размер изображения = ГН

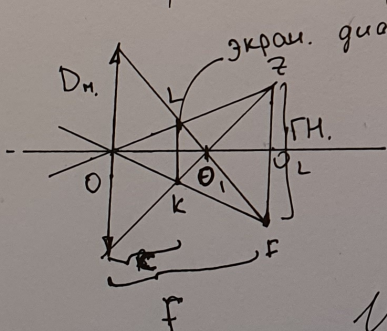
Из подобия

$\Delta ABC \sim \Delta DEC$

$\frac{b}{x} = \frac{ГН}{D_n} \Rightarrow D_n = \frac{ГН \cdot x}{b}$

$D_n = \frac{\frac{1}{3} \cdot 9 \cdot 36}{24} = \frac{3 \cdot 36^2}{24 \cdot 3} = 4,5 \text{ см}$

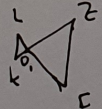
3) Построим ход лучей после линзы.



$\frac{OO_1}{O_1O_2} = \frac{ГН \cdot x}{b \cdot ГН} = \frac{x}{b} = \frac{36}{24} = \frac{3}{2}$

$OO_1 = \frac{2}{5} f \quad O_1O_2 = \frac{2}{5} f$

Из подобия треугольников  $\Delta KLO_1 \sim \Delta OZF$



$\frac{a}{ГН} = \frac{OO_1 - c}{O_1O_2} \Leftrightarrow \frac{a}{ГН} = \frac{\frac{2}{5}f - c}{\frac{2}{5}f}$

Из подобия  $\Delta OZF \sim \Delta CLK \quad \frac{a}{ГН} = \frac{c}{f}$

$\frac{\frac{2}{5}f - c}{\frac{2}{5}f} = \frac{c}{f} \Rightarrow 3f - 5c = 2c \Rightarrow 3f = 7c \Rightarrow c = \frac{3f}{7} = \frac{3dF}{7(d-F)} = \frac{3 \cdot 36 \cdot 9}{7 \cdot 24} = 5,1 \text{ см}$

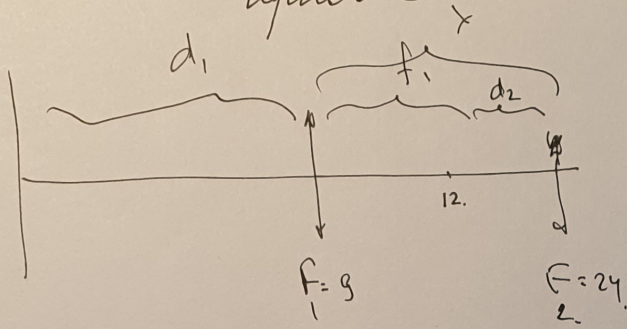
$c = \frac{36}{7} = 5,1 \text{ см}$

Ответ: 1) X = 36 см 2) D<sub>н</sub> = 4,5 3) за линзой на 5,1 см

3



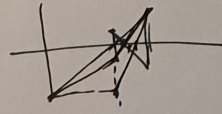
Чепухов



$$\frac{a}{\Gamma H} = \frac{00_1 - c}{0_1 0_2}$$

$$\frac{D_{H1}}{a} = \frac{00_1}{00_1 - c}$$

$$\frac{f}{c} = v$$

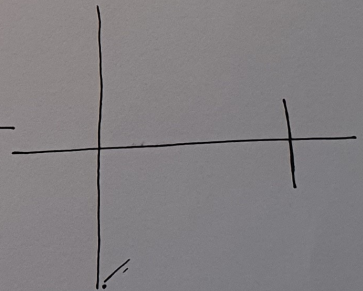
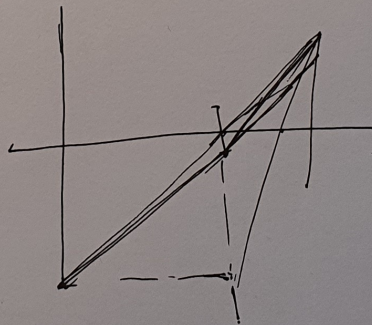
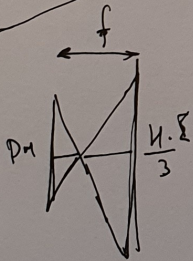
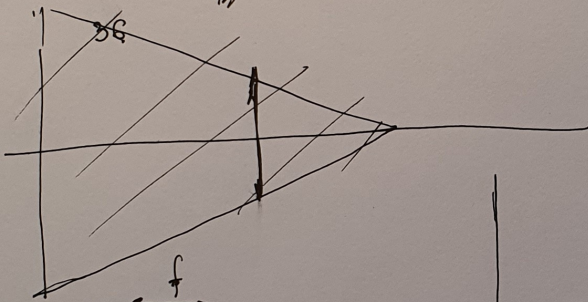
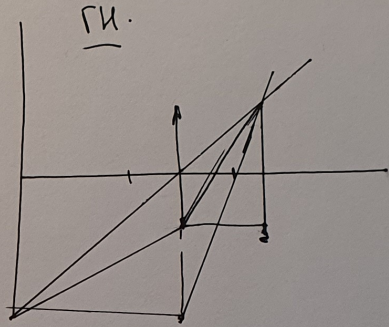
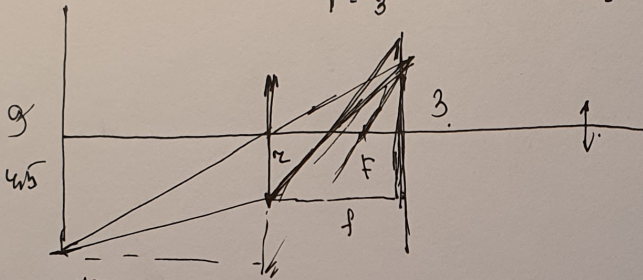
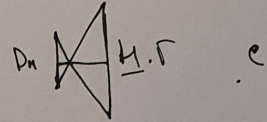


$$\frac{c}{f} = \frac{a}{\Gamma H}$$

$$f = \frac{d F_1}{d - F_1} = \frac{36 \cdot 9}{27} = 12$$

$$\Gamma = \frac{1}{3}$$

$$-f_1 + d_2 = x$$

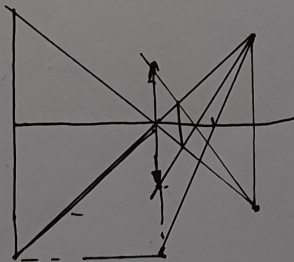
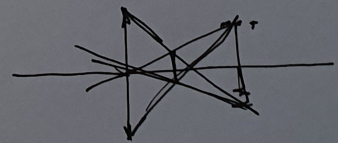
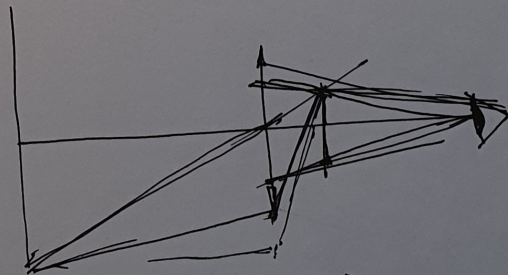


$$\frac{f}{3} \times 3 D_n = f$$

$$\frac{D_n}{\frac{4}{3}} = \frac{x}{f-x}$$

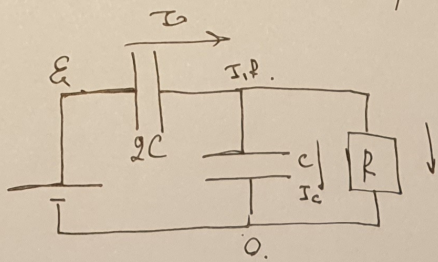
$$3 D_n f - 3 D_n x = 4x$$

$$3 D_n f = (4 + 3 D_n) x$$





Черновик



$$\frac{2C(\varepsilon - \varphi)}{\Delta t} = \frac{C\varphi}{\Delta t} + I$$

$$\frac{2C(\varepsilon - \varphi)}{\Delta t} = I_0$$

$$I = \frac{\varphi}{R}$$

$\frac{d\varphi}{dt}$

$$\frac{2C(\varepsilon - I_1 R)}{\Delta t} = I_0$$

$$\frac{2C(\varepsilon - I_1 R)}{\Delta t} - \frac{I_1 R C}{\Delta t} = I_1$$

$$2\varepsilon - I_1 R = I_0 \Delta t$$

$2C\varepsilon$

$$2C\varepsilon - I_0 \Delta t = I_1 R \cdot 2C \Rightarrow I_1 R C = 2C\varepsilon - \frac{I_0 \Delta t}{2}$$

$$I_0 = \frac{C\varepsilon}{\Delta t}$$

$$I_0 = \left( \frac{C}{\Delta t} R + 1 \right) I_1$$

$$I_0 = \frac{2C(\varepsilon - I_1 R)}{\Delta t}$$

$$I_1 \frac{CR + \Delta t}{\Delta t} = \frac{2C\varepsilon - 2CI_1 R}{\Delta t}$$

$$I_1 R + \Delta t = \frac{2C\varepsilon - 2CI_1 R}{I_1}$$

$$\Delta t = \frac{2C\varepsilon}{I_1} - 3CR$$

$$I_0 = \frac{2C(\varepsilon - I_1 R) \cdot I_1}{2C\varepsilon - 3CRI_1}$$

$$2\varepsilon I_0 - 3RI_1 I_0 = 2\varepsilon I_1 - 2I_1^2 R$$

$$2I_1^2 R - (3RI_1 + 2\varepsilon) I_1 + 2\varepsilon I_0 = 0$$

$$D = 9RI_0^2 + \varepsilon^2 + 24RI_0\varepsilon$$

$$I_0 = \frac{C I_1 R}{\Delta t} + I_1$$

$$I_0 = \frac{2C\varepsilon - I_1 R}{\Delta t}$$

$$CI_1 R + I_1 \Delta t = 2C\varepsilon - I_1 R$$

$$I_0 = \frac{C d\varphi}{dt} + I_1$$

$$I_0 \cdot \frac{d\varphi}{dt}$$

$\varphi - C$

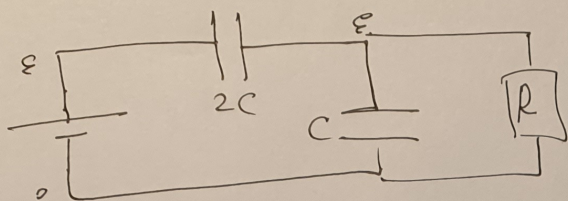
$$\frac{q}{C} = \ddot{u}$$

$$\frac{I_0}{2C} = \dot{u} + 1$$

$$\frac{I_0}{2C} \downarrow \downarrow$$

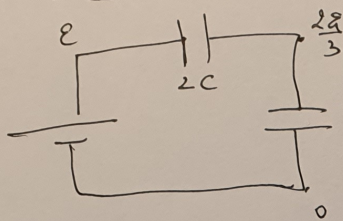


Меробук  
N3



Упр. 4. C ↑ во 3.

$$I_0 - \frac{C\varphi}{\Delta t} = I$$



$$2C(\varepsilon - \varphi) = C\varphi$$

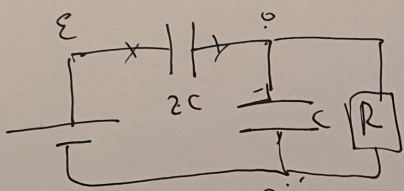
$$2\varepsilon = 3\varphi \Rightarrow$$

$$\frac{2\varepsilon}{3} = \varphi$$

$$I_0 - \frac{C\varphi}{\Delta t} + I_0 = I$$

$$2I_0 - \frac{C\varphi}{\Delta t} = I$$

$$I = \frac{2\varepsilon}{3R}$$



$$\varphi_1 - I_1 R = \frac{q_1}{C}$$

$$(0 - I_1)R =$$

$$C\dot{\varphi} = I_0$$

$$I_1 R = \frac{q_1}{C}$$

$$\frac{2C(\varepsilon - \varphi_1)}{\Delta t} = \frac{C(\varphi_1)}{\Delta t} + I$$

$$\frac{C(\varepsilon - \varphi_1)}{\Delta t} = I_0$$

$$\frac{2C\varepsilon - 2C\varphi_1}{\Delta t} = I$$

$$C\varepsilon - \varphi_1 = I_0 \Delta t$$

$$C\varepsilon - I_0 \Delta t = C\varphi_1$$

N4.

$$\mathcal{E}_A \pm BvL$$

$$I = \frac{BvL}{3R}$$

$$2ma = F_A = BIL = \frac{B^2 L^2 v}{3R}$$

$$a = \frac{B^2 L^2 v}{6Rm}$$

$$\mathcal{E}_{i2} = Bu_2 L \quad \mathcal{E}_{i1} = Bu_1 L$$

$$3eU \quad \frac{v}{3} \quad ;$$

3) Суммарно

$$\mathcal{E}_i = Bu_2 L$$

$$\mathcal{E}_i = Bu_1 L$$

