

# Часть 1

Олимпиада: **Физика, 11 класс (1 часть)**

Шифр: **21200366**

ID профиля: **177367**

Вариант 4

(Проблем)  
Вариант 11-04

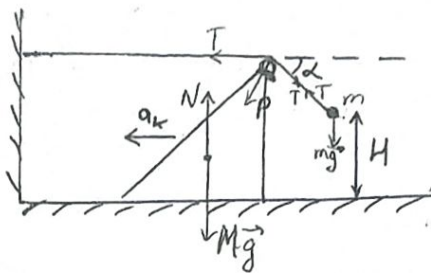
Условие.

Рязань МКУ

№1 Дано:

$$\alpha, \cos \alpha = \frac{8}{17}, H$$

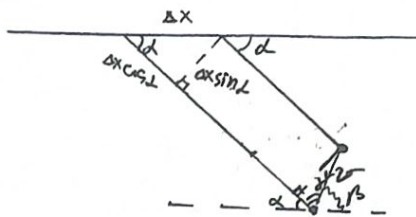
- 1)  $\operatorname{tg} \beta$  - ?
- 2)  $a_x$  - ?
- 3)  $\frac{m}{M}$  - ?
- 4)  $\tau$  - ?



$$\cos \alpha = \frac{8}{17}$$

$$\sin \alpha = \sqrt{1 - \cos^2 \alpha} = \sqrt{1 - \frac{64}{289}} = \sqrt{\frac{225}{289}} = \frac{15}{17}$$

$$\operatorname{tg} \alpha = \frac{\sin \alpha}{\cos \alpha} = \frac{15 \cdot 17}{17 \cdot 8} = \frac{15}{8}$$



$a \uparrow \Rightarrow \beta$  - увеличился

$$1) \operatorname{tg} \beta = \frac{\Delta x \sin \alpha}{\Delta x (1 - \cos \alpha)} = \frac{\sin \alpha}{1 - \cos \alpha} = \frac{15}{17 \cdot (1 - \frac{8}{17})} = \frac{15 \cdot 17}{17 \cdot 9} = \frac{15}{9}$$

$$\operatorname{tg}(\alpha + \beta) = \frac{\operatorname{tg} \alpha + \operatorname{tg} \beta}{1 - \operatorname{tg} \alpha \cdot \operatorname{tg} \beta} = \frac{\frac{15}{8} + \frac{15}{9}}{1 - \frac{225}{72}} = -\frac{15 \cdot 72}{72 \cdot 153} = -\frac{15}{153}$$

$$\operatorname{tg} \beta = \operatorname{tg}(180 - (\alpha + \beta)) = -\operatorname{tg}(\alpha + \beta) = \frac{15}{153}$$

2)

Ответ: 1)  $\operatorname{tg} \beta = \frac{15}{153}$

①

№2 Дано:

$$\nu(\text{He}), T_0, C(T) = \frac{9}{5}R \frac{T}{T_0}$$

- 1)  $Q_1 (Q_1 > 0) - ? \quad T_1 = \frac{3}{4}T_0$
- 2)  $A_{\min} \quad T_k - ?$
- 3)  $A_{\min} - ?$

Решение:

Температура - одинаковая. уг. раз  $\Rightarrow C_v = \frac{3}{2}R, C_p = \frac{5}{2}R$

По первому началу м/г:

$$Q_+ = \Delta U + A$$

$$1) \Delta U = C_v \nu (T_1 - T_0) = \frac{3}{2} \nu R (T_1 - T_0) = \frac{3}{2} \nu R (\frac{3}{4}T_0 - T_0) = -\frac{3\nu R T_0}{8}$$

$$\nu C dT = \nu C_v dT + dA$$

$$dA = \nu (C - C_v) dT$$

$$\int_0^A dA = \int_{T_0}^{T_1} \nu (\frac{9R}{5T_0} T - \frac{3}{2}R) dT$$

$$A = \int_{T_0}^{T_1} (\frac{9\nu R}{5T_0} T dT - \frac{3}{2}\nu R dT)$$

$$A = \frac{9\nu R}{10T_0} (T_1^2 - T_0^2) - \frac{3}{2}\nu R (T_1 - T_0) = \frac{9\nu R}{10T_0} (\frac{9}{16}T_0^2 - T_0^2) -$$

$$-\frac{3}{2}\nu R (\frac{3}{4}T_0 - T_0) = -\frac{9 \cdot 7 \nu R T_0^2}{10 \cdot 16 T_0} + \frac{3\nu R T_0}{8} = -\frac{63}{160}\nu R T_0 + \frac{3}{8}\nu R T_0 = \frac{-63+60}{160}\nu R T_0 = -\frac{3}{160}\nu R T_0$$

$$Q = \Delta U + A = -\frac{3\nu R T_0}{8} - \frac{3}{160}\nu R T_0 = -\frac{63\nu R T_0}{160} \text{ - тепло, переданное газу } \Rightarrow$$

$$\Rightarrow Q_1 = -Q = \frac{63\nu R T_0}{160}$$

$$2) A = \frac{9\nu R}{10T_0} (T_k^2 - T_0^2) - \frac{3}{2}\nu R (T_k - T_0) = \frac{3}{2}\nu R (T_k - T_0) \left( \frac{3(T_k + T_0)}{5T_0} - 1 \right) = \frac{3}{2}\nu R (T_k - T_0) \left( \frac{3T_k - 2T_0}{5T_0} \right) =$$

$$= \frac{3}{2}\nu R \cdot \frac{3T_k^2 - 2T_k T_0 - 3T_0 T_k + 2T_0^2}{5T_0} = \frac{3}{2}\nu R \frac{3T_k^2 - 5T_k T_0 + 2T_0^2}{5T_0}$$

$$A(T_k) = \frac{3\nu R}{10T_0} (3T_k^2 - 5T_k T_0 + 2T_0^2)$$

$$A_{\min} \rightarrow T_k = -\frac{(-5T_0)}{2 \cdot 3} = \frac{5T_0}{6}$$

$$3) A_{\min} = \frac{3\nu R}{10T_0} \left( 3 \cdot \frac{25T_0^2}{36} - \frac{25T_0^2}{6} + 2T_0^2 \right) = \frac{3\nu R}{10T_0} \left( \frac{25T_0^2}{12} - \frac{50T_0^2}{12} + \frac{24T_0^2}{12} \right) = \frac{3\nu R}{10T_0} \cdot \left( -\frac{T_0^2}{12} \right) =$$

$$= -\frac{\nu R T_0}{40}$$

Ответ: 1)  $Q_1 = \frac{63\nu R T_0}{160}$

2)  $T_k = \frac{5T_0}{6}$

3)  $A_{\min} = -\frac{\nu R T_0}{40}$

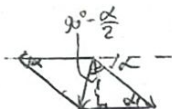
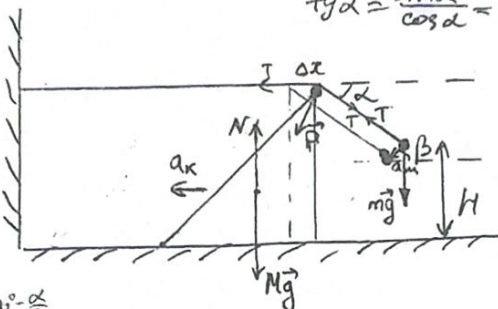
(2)

# Упробук.

x/z

$$\sin \alpha = \sqrt{1 - \cos^2 \alpha} = \sqrt{1 - \frac{64}{289}} = \sqrt{\frac{225}{289}} = \frac{15}{17}$$

$$\operatorname{tg} \alpha = \frac{\sin \alpha}{\cos \alpha} = \frac{15 \cdot 17}{17 \cdot 8} = \frac{15}{8}$$



$$P_y = T \sin \alpha$$

$$P_x = T - T \cos \alpha = T(1 - \cos \alpha)$$

$$90^\circ - \frac{\alpha}{2} - 90^\circ + \alpha = P_x = T(1 - \cos \alpha) = M a_x$$

$$= \frac{\alpha}{2}$$

$$T \cos \alpha = M a_x \quad T \cos \alpha = M a_x$$

$$T \sin \alpha = m g$$

$$T \cos \alpha = M a_x$$

$$T \cos \alpha = M a_x$$

Чт

$$\int C \Delta T = \frac{3}{2} V R \Delta T + p \Delta V$$

$$\int (C - \frac{3}{2} p R) \Delta T = p \Delta V = A$$

$$\int (C - \frac{3}{2} p R) dT = dA$$

$$\int_{T_0}^{T_1} (\frac{3}{5} R \frac{T}{T_0} - \frac{3}{2} p R) dT = dA$$

$$\int dA = \int_{T_0}^{T_1} (\frac{3}{5} R \frac{T}{T_0} - \frac{3}{2} p R) dT$$

$$A = \left. \frac{3}{5} R \frac{T^2}{2 T_0} + \frac{3}{2} p R T \right|_{T_0}^{T_1} = \frac{3}{10} R \frac{T_1^2 - T_0^2}{T_0} + \frac{3}{2} p R (T_1 - T_0) = \frac{3}{2} p R (T_1 - T_0) \left( \frac{3}{5} \frac{T_1 + T_0}{T_0} - 1 \right) =$$

$$= \frac{3}{2} p R (T_1 - T_0) \left( \frac{3 T_1 + 3 T_0 - 5 T_0}{5 T_0} \right) = \frac{3}{2} p R (T_1 - T_0) \left( \frac{3 T_1 - 2 T_0}{5 T_0} \right) = \frac{3}{2} p R \left( \frac{3 T_1^2 - 2 T_1 T_0 - 3 T_1 T_0 + 2 T_0^2}{5 T_0} \right) =$$

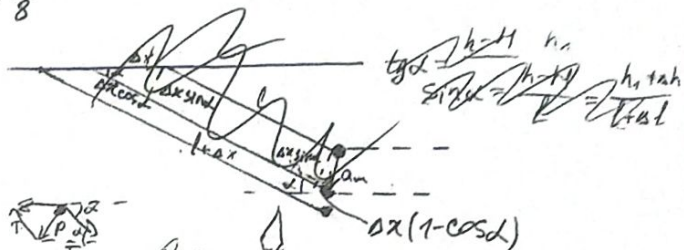
$$= \frac{3}{2} p R \left( \frac{3 T_1^2 - 5 T_1 T_0 + 2 T_0^2}{5 T_0} \right) \quad - \frac{b}{2a} = \frac{5 T_0}{6}$$

$$A_{\min} = \frac{3}{2} p R \left( \frac{3 \cdot \frac{25}{36} T_0^2 - \frac{25}{6} T_0^2 + 2 T_0^2}{5 T_0} \right) = \frac{3}{2} p R \left( \frac{25}{12} T_0^2 - \frac{25}{6} T_0 + 2 T_0^2 \right) =$$

$$= \frac{3 p R}{2 \cdot 5 T_0} (25 T_0^2 - 50 T_0^2 + 24 T_0^2) = \frac{3 p R}{10 T_0} (-T_0^2) = -\frac{3 p R T_0}{10}$$

$$-\frac{3 p R T_0^2}{10 \cdot 12} = -\frac{p R T_0}{40}$$

$$M U_x \neq m U_{ux} = 0$$



$$T \sin \alpha - m g = m a_y$$

$$T \cos \alpha = m a_x$$

$$T \sin \alpha = m(g + a_x)$$

$$\operatorname{tg} \alpha = \frac{g + a_x}{a_y}$$

$$a_y \operatorname{tg} \alpha = g + a_x = \frac{\sin \alpha}{\cos \alpha} = \frac{\sin \alpha \cos \beta + \cos \alpha \sin \beta}{\cos \alpha \cos \beta} =$$

$$= \frac{\sin(\alpha + \beta)}{\cos \alpha \cos \beta} =$$

$$\operatorname{tg}(180^\circ - \alpha) = -\operatorname{tg} \alpha$$

$$\operatorname{tg}(\alpha + \beta) = \frac{\sin(\alpha + \beta)}{\cos(\alpha + \beta)} = \frac{\sin \alpha \cos \beta + \cos \alpha \sin \beta}{\cos \alpha \cos \beta - \sin \alpha \sin \beta} = \frac{\operatorname{tg} \alpha + \operatorname{tg} \beta}{1 - \operatorname{tg} \alpha \operatorname{tg} \beta}$$

$$= \frac{\frac{15}{8} + \frac{15}{4}}{1 - \frac{225}{72}} = \frac{15 \cdot 72}{72 \cdot (72 - 225)} = -\frac{15}{153}$$

$$\operatorname{tg} \beta = -\operatorname{tg}(\alpha + \beta) = \frac{15}{153}$$



# Часть 2

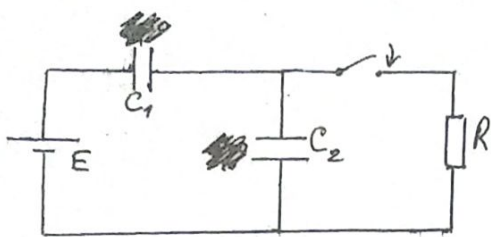
Олимпиада: **Физика, 11 класс (2 часть)**

Шифр: **21200366**

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Вариант 4

№3



(предварительно не заряжены)

Дано:  $q_{c0} = q_{2c0} = 0, C, R$

$C_2 = C, C_1 = 5C$

Найти: 1)  $I_{R0} - ?$

2)  $Q - ?$

3)  $I_R - ? I_{C2} = I_0$

1) До замыкания ключа режим установился  $\Rightarrow$  тока нет

II з-н Кирхгофа:  $E = \frac{q_1}{C_1} + \frac{q_2}{C_2}$   $q_0 = q_1 = q_2$  (послед. соединение)

$$E = \frac{q_0}{5C} + \frac{q_0}{C} = \frac{q_0}{5C} + \frac{5q_0}{5C} = \frac{6q_0}{5C} \Rightarrow \frac{q_0}{C} = \frac{5E}{6}, q_0 = \frac{5}{6}EC$$

Сразу после замыкания ключа напряжение на конденсаторах будет такое же, как и до размыкания  $\Rightarrow U_{C2} = \frac{q_0}{C_2} = \frac{q_0}{C} = \frac{5E}{6}$

$$U_{C2} = I_{R0} \cdot R \Rightarrow I_{R0} = \frac{U_{C2}}{R} = \frac{5E}{6R}$$

2) После замыкания ключа, когда режим установился, тока нет  $\Rightarrow$

$$\Rightarrow IR = 0 \Rightarrow U_{C2} = IR = 0$$

$$E = U_{C1} = \frac{q_1}{C_1} \Rightarrow q_1 = 5EC$$

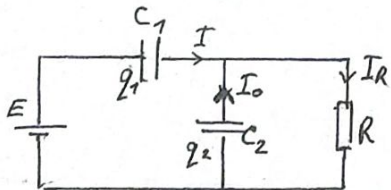
По ЭСЭ:  $E \Delta q = \Delta W_{C1} + \Delta W_{C2} + Q$

$$\Delta q = q_1 - q_0 = 5EC - \frac{5}{6}EC = \frac{25}{6}EC \quad \Delta W_{C1} = \frac{q_1^2}{2C_1} - \frac{q_0^2}{2C_1} = \frac{25E^2C^2}{10C} - \frac{25E^2C^2}{36C} = \frac{25E^2C^2 \cdot 36 - 25E^2C^2 \cdot 10}{360} = \frac{25E^2C^2 \cdot 26}{72}$$

$$\Delta W_{C2} = 0 - \frac{q_0^2}{2C_2} = -\frac{25E^2C^2}{36 \cdot 2C} = -\frac{25E^2C}{72}$$

$$Q = E \Delta q - \Delta W_{C1} - \Delta W_{C2} = \frac{25}{6}E^2C - \frac{175E^2C}{72} + \frac{25E^2C}{72} = \frac{300E^2C - 175E^2C + 25E^2C}{72} = \frac{150E^2C}{72} = \frac{50E^2C}{24} = \frac{25E^2C}{12}$$

3)



По 2 правую Кирхгофа:

$$E = U_{C1} + U_{C2}$$

По 1 правую Кирхгофа:

$$I = I_R - I_0$$

$$q_1 = I = I_R - I_0 \quad q_2 = -I_0$$

$$E = U_{C1} + U_{C2} = \frac{q_1}{C_1} + \frac{q_2}{C_2}$$

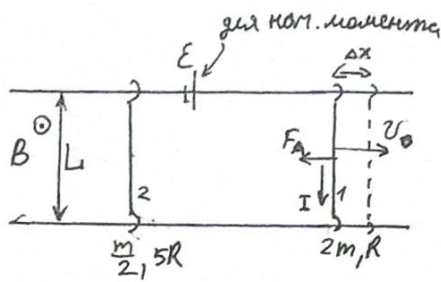
Продифференцируем:

$$\dot{E} = \frac{\dot{q}_1}{5C} + \frac{\dot{q}_2}{C} \Rightarrow 0 = \frac{I_R - I_0}{5C} - \frac{I_0}{C} = \frac{I_R - 6I_0}{5C} \Rightarrow I_R = 6I_0$$

Ответ: 1)  $I_{R0} = \frac{5E}{6R}$ , 2)  $Q = \frac{25}{12}CE^2$ , 3)  $I_R = 6I_0$

(1)

№4



Дано:  $B, L, m_1 = 2m, R_1 = R, v_0$   
 $m_2 = \frac{m}{2}, R_2 = 5R$

Найти: 1)  $a_{1.0} - ?$

2)  $v_1, v_2 - ?$

3)  $\Delta L - ?$

~~1) В начальный момент на перемычку (на проводник) зарядят в ней генератор  $F_A$  сила Лоренца  $\Rightarrow$  возникает эл. ток~~

1) по 3-му закону Фарадея:  $-\frac{d\Phi}{dt} = \epsilon = -\frac{BL dx}{dt} = -BLv_0$

$$\epsilon = I(R_1 + 5R) = 6IR \Rightarrow I = \frac{BLv_0}{6R}$$

$$F_A = BIL = \frac{(BL)^2 v_0}{6R} = 2ma_{1.0} \Rightarrow a_{1.0} = \frac{(BL)^2 v_0}{12mR}$$

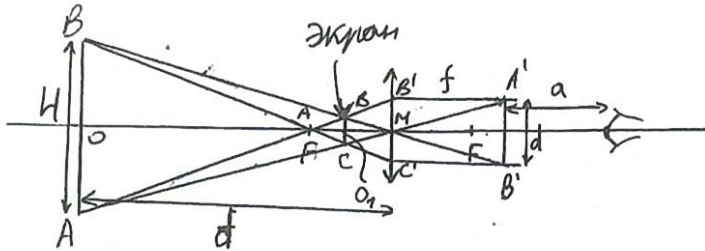
2)

Ответ: 1)  $a_{1.0} = \frac{(BL)^2 v_0}{12mR}$

(2)

Чистовик.

№5



Дано:

$$F = 24 \text{ см}$$

$$H = 9 \text{ см}$$

$$d = 96 \text{ см}$$

$$d' = 24 \text{ см}$$

1)  $x - ?$

2)  $D_m - ?$

3)  $l - ?$

1) По ф-ле тонкой линзы:

$$\frac{1}{d} + \frac{1}{f} = \frac{1}{F} \Rightarrow \frac{1}{f} = \frac{d-F}{Fd} \Rightarrow f = \frac{Fd}{d-F} = \frac{24 \cdot 96}{96-24} = \frac{24 \cdot 96}{72} = 32 \text{ см} - \text{рассто-}$$

яние от линзы до изображения

$$x = f + a = 32 + 24 = 56 \text{ см}$$

2)  $\Gamma_1 = \frac{d}{D} = \frac{f}{d} \Rightarrow d = D \frac{f}{d} = \frac{96}{96} \cdot 9 \cdot \frac{32}{96} = 9 \cdot \frac{1}{3} = 3 \text{ см}$

При  $D_m = d = 3 \text{ см}$  наблюдатель сможет увидеть целиком всё изображение гипербола

3) Из подобия  $\triangle ABC \sim \triangle B'C' \Rightarrow$

$$\triangle OBM \sim \triangle O_1BM \Rightarrow \frac{H}{2b} = \frac{d}{l}$$

$$\triangle ABM \sim \triangle AO_1M \Rightarrow \frac{d}{2b} = \frac{F}{F-l}$$

$$\Rightarrow \frac{H}{d} = \frac{d(F-l)}{lF} \Rightarrow$$

$$\Rightarrow HlF = d^2F - d^2l \Rightarrow (HlF + d^2l) = d^2F \Rightarrow l = \frac{d^2F}{HF + d^2} = \frac{9 \cdot 24}{9 \cdot 24 + 9} = \frac{9 \cdot 24}{9 \cdot 25} = \frac{24}{25} \text{ см}$$

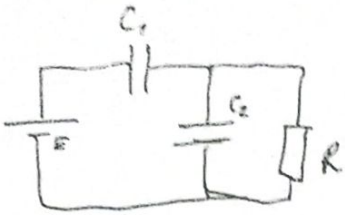
Ответ: 1)  $x = 56 \text{ см}$

2)  $D_m = 3 \text{ см}$

3)  $l = \frac{24}{25} \text{ см}$



Чепробук:



$$E = U_{C1} + U_{C2} \quad U_{C2} = IR$$

$$E = \frac{q_1}{C_1} + \frac{q_2}{C_2} = \frac{q}{5C} + \frac{q}{C} = \frac{6q}{5C}$$

$$\frac{q}{C} = IR$$

$$E = U_{C1} + U_{C2}$$

$$U_{C2} = IR$$

$$U_{C2} = 0 \quad E = \frac{q_1}{C_1} = \frac{q_1}{5C} \Rightarrow q_1 = 5CE$$

$$EI = IR(I) + U_{C2}I_0 \quad E = U_{C1} + U_{C2} \quad EI = U_{C1}I + U_{C2}I$$

$$U_{C2}I_0 = IR$$

$$EI = U_{C1}I + U_{C2}I_0 + I^2R$$

$$U_{C2}I_0 = U_{C2}I_0 + I^2R$$

$$U_{C2}(I - I_0) = I^2R$$

$$U_{C2}IR = I^2R$$

$$E(I - I_0) = U_{C1}(I - I_0) + U_{C2}I_0$$

$$E = \frac{q_1}{C_1} + \frac{q_2}{C_2}$$

$$q_2 = I_0$$

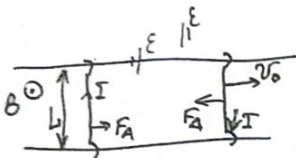
$$q_1 = I_0 + IR$$

$$E = \frac{q_1}{C_1} + \frac{q_2}{C_2}$$

$$0 = \frac{I_0 + IR}{5C} + \frac{I_0}{C} = \frac{6I_0 + IR}{5C} = 0 \Rightarrow IR = 6I_0$$

$$q_2 = -I_0$$

$$\frac{IR - I_0}{5C} + \frac{I_0}{C} = \frac{IR - I_0 - 5I_0}{5C} = \frac{IR - 6I_0}{5C} = 0$$

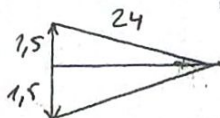
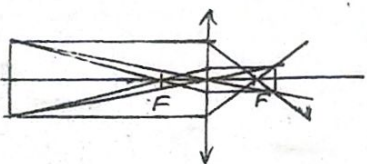
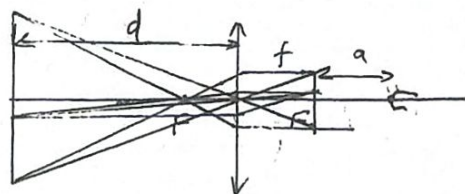
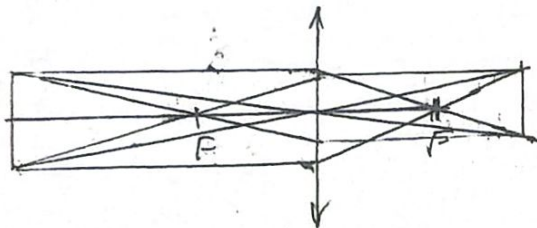


$$F = IBL \quad F_A = IBL = ma$$

$$a = \frac{IBL}{m}$$

$$- \frac{BLdx}{dt} = \mathcal{E} \Rightarrow \mathcal{E} = BLv$$

$$\mathcal{E} = I(R + r)$$



$$\frac{d}{D} = \frac{f}{d}$$

$$d = D \frac{f}{d} = \frac{32}{96} D = \frac{D}{3}$$

$$\sqrt{24^2 - 1.5^2} = \sqrt{576 - 2.25} = \sqrt{573.75} \stackrel{5cm}{=} 23.95 \approx 24$$

$$l = \frac{2bd}{4f}$$

$$\frac{H}{d} = \frac{d(F-l)}{lF}$$

$$\frac{b^2}{d} = \frac{F-l}{l}$$