

# Часть 1

Олимпиада: **Физика, 11 класс (1 часть)**

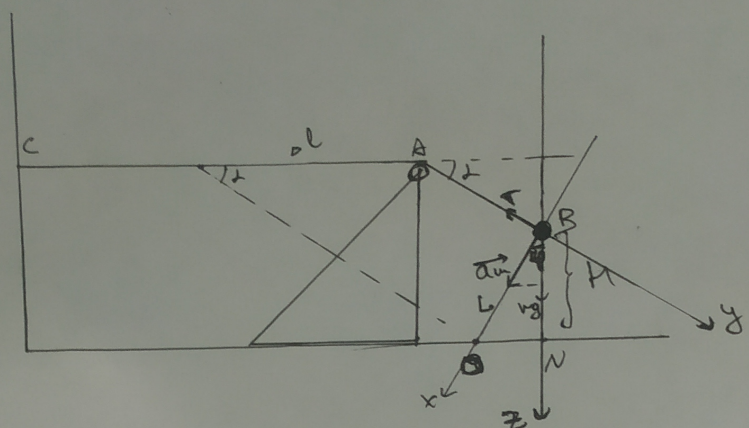
Шифр: **21202524**

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Вариант 4

~1

- $\cos \alpha = \frac{8}{17}$
- M
- 1)  $\varphi$  - ?
  - 2)  $a_{\text{кр}}$  - ?
  - 3)  $\frac{m}{M}$  - ?
  - 4)  $t$  - ?



1) т.к.  $L = \text{const}$ , т.е. угловое перемещение ~~не~~ не зависит на  $L$ , то  $\vec{a}_{\text{кр}} \perp \vec{v}$ , т.е.  $\varphi = \alpha$  и  $\cos \varphi = \cos \alpha = \frac{8}{17}$

2) Пусть  $OB = L$ , тогда непрерывное движение:  $\alpha l$  и  $\sin \alpha = \frac{L}{\alpha l}$

~~также~~ ~~не~~ ~~есть~~ ~~cos~~ тогда  $L = \alpha l \sin \alpha$ , т.е.  $a_{\text{кр}} = a_{\text{кр}} \cdot \sin \alpha$

$a_{\text{кр}} = \frac{a_{\text{кр}}}{\sin \alpha}$

3, Нормальная на оси:  $Ox: m a_{\text{кр}} = m g \cos \alpha$

(оси, как показано на рис.)  $Oy: T = m g \sin \alpha$

$\Rightarrow a_{\text{кр}} = g \cos \alpha$  тогда  $a_{\text{кр}} = \frac{g \cos \alpha}{\sin \alpha} = g \cdot \frac{1}{\text{tg} \alpha} = g \cdot \frac{8}{15} \approx 5,3 \text{ м/с}^2$

$\sin \alpha = \sqrt{1 - \frac{64}{289}} = \frac{15}{17}$

$\text{tg} \alpha = \frac{15}{8}$

3)

4)  $H = \frac{a_{\text{кр}} t^2}{2}$ , где  $a_{\text{кр}} = a_{\text{кр}} \cdot \cos \alpha = g \cos^2 \alpha$

$$\frac{2H}{g \cos^2 \alpha} = t^2 \quad t = \sqrt{\frac{2H}{g \cos^2 \alpha}} = \frac{\sqrt{2}}{\sqrt{g} \cos \alpha} \cdot \sqrt{H} = \frac{\sqrt{2}}{8 \cdot \frac{15}{17}} \sqrt{H} \approx 0,95 \sqrt{H}$$

Ответ: 1)  $\cos \varphi = \frac{8}{17}$ ; 2)  $a_{\text{кр}} = \frac{8}{15} g \approx 5,3 \text{ м/с}^2$ ; 3) —; 4)  $t = \sqrt{\frac{2H}{g \cos^2 \alpha}} \approx 0,95 \sqrt{H}$

✓2

$\nu$
$\nu_0$
$C(\nu) = \frac{9}{5} R \frac{\nu}{\nu_0}$
1) $Q_1$ ?
2) $\nu$ ?
3) $A_{min}$ ?

1)  $dQ = \nu C dT$

$$dQ = \nu \cdot \frac{9}{5} R \frac{\nu}{\nu_0} dT$$

$$\Rightarrow |Q_1| = \left| \frac{9}{5} \frac{\nu R}{\nu_0} \cdot \frac{\nu^2}{2} \Big|_{\nu_0}^{\frac{7}{16}\nu_0} \right| \Rightarrow Q_1 = \frac{9}{5} \frac{\nu R}{\nu_0} \left( \frac{\nu_0^2}{2} - \frac{9}{16} \nu_0^2 \right)$$

$$Q_1 = \frac{9}{10} \frac{\nu R}{\nu_0} \cdot \nu_0^2 \left( \frac{7}{16} \right) ; Q_1 = \frac{63}{160} \nu R \nu_0$$

2)  $dA = dQ - dU$  (из 2 начала термодинамики) ;  $dU = \frac{3}{2} \nu R dT$

$$dA = \frac{9}{5} \frac{\nu R}{\nu_0} \nu dT - \frac{3}{2} \nu R dT \Rightarrow A = \frac{9}{10} \frac{\nu R}{\nu_0} (\nu^2 - \nu_0^2) - \frac{3}{2} \nu R (\nu - \nu_0)$$

$$A = \frac{9}{10} \frac{\nu R}{\nu_0} \cdot \nu^2 - \frac{3}{2} \nu R \nu - \frac{9}{10} \nu R \nu_0 + \frac{3}{2} \nu R \nu_0$$

$$A(\nu) = \frac{9}{10} \frac{\nu R}{\nu_0} \nu^2 - \frac{3}{2} \nu R \nu + \frac{6}{10} \nu R \nu_0$$

$$A'(\nu) = \frac{9}{10} \frac{\nu R}{\nu_0} \cdot 2\nu - \frac{3}{2} \nu R ; \text{ при } A_{min} \quad A'(\nu) = 0, \text{ т.е.}$$

$$\frac{18}{10} \frac{\nu R}{\nu_0} \cdot \nu - \frac{3}{2} \nu R = 0 \Rightarrow \frac{18}{10} \frac{\nu}{\nu_0} = \frac{3}{2} \Rightarrow \nu = \frac{3}{2} \cdot \frac{10}{18} \nu_0 = \frac{5}{6} \nu_0$$

$$\nu = \frac{5}{6} \nu_0$$

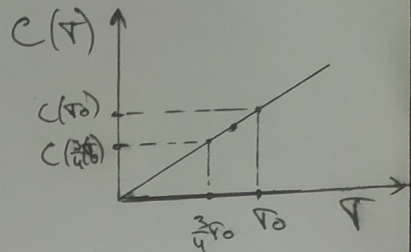
3) 
$$A_{min} = A\left(\nu = \frac{5}{6} \nu_0\right) = \frac{9}{10} \frac{\nu R}{\nu_0} \cdot \frac{25}{36} \nu_0^2 - \frac{3}{2} \nu R \cdot \frac{5}{6} \nu_0 + \frac{6}{10} \nu R \nu_0 =$$
$$= 0,625 \nu R \nu_0 - 1,25 \nu R \nu_0 + 0,6 \nu R \nu_0 = -0,025 \nu R \nu_0$$

$$\text{Ответ: 1) } Q_1 = \frac{63}{160} \nu R \nu_0 \approx 0,4 \nu R \nu_0 ; 2) \nu = \frac{5}{6} \nu_0 \approx 0,83 \nu_0 ; 3) A_{min} = -0,025 \nu R \nu_0$$

$\frac{V}{T}$   
 $C(T) = \frac{9}{5} R \frac{T}{T_0}$

1)  $Q = \int C dT$        $C(T) = \frac{9}{5} R \frac{T}{T_0}$

~~$Q = \int_{T_0}^{T_0 + \frac{3}{4} T_0} C(T) dT = \frac{9}{5} R \frac{T_0 + \frac{3}{4} T_0}{T_0}$~~



1)  $T_0 \rightarrow \frac{3}{4} T_0$

$Q_1 = ?$

2)  $T = ?$   $A_{min}$

3)  $A_{min} = ?$

~~$C_p$~~

$dQ = \int \frac{9}{5} R \frac{T}{T_0} dT$

$dQ = \frac{9}{5} \frac{R}{T_0} T dT$

$Q = \frac{9}{5} \frac{R}{T_0} \frac{T^2}{2}$

$Q_1 = \frac{9}{5} \frac{R}{T_0} \frac{T^2}{2} \Big|_{T_0}^{\frac{3}{4} T_0}$

$Q = \frac{9}{5} \frac{R}{T_0} \cdot \frac{(T_0^2 - \frac{9}{16} T_0^2)}{2}$

$Q_1 = \frac{9}{5} \frac{R}{T_0} \frac{7 T_0^2}{32}$

$Q = \frac{63}{160} R T_0$

2)  $A = Q - U$

$dA = dQ - dU$  ;  $dA = \frac{9}{5} \frac{R}{T_0} T dT - \frac{3}{2} R dT$

$A = \frac{9}{5} \frac{R}{T_0} \cdot \frac{T^2}{2} \Big|_{T_0}^T - \frac{3}{2} R T \Big|_{T_0}^T$

$A = \frac{9}{10} \frac{R}{T_0} \frac{(T^2 - T_0^2)}{2} - \frac{3}{2} R (T - T_0)$

$A(T) = \frac{9}{10} \frac{R}{T_0} (T^2 - T_0^2) - \frac{3}{2} R (T - T_0)$

$A(T) = \frac{9}{10} \frac{R}{T_0} T^2 - \frac{9}{10} \frac{R}{T_0} T_0^2 - \frac{3}{2} R T + \frac{3}{2} R T_0$

$A(T) = \frac{9}{10} \frac{R}{T_0} T^2 - \frac{3}{2} R T + \frac{6}{10} R T_0$

$T_0 = \frac{\frac{3}{2} R T_0}{\frac{2 \cdot \frac{9}{10} R}{10}} = \frac{3 \cdot 10^5}{2 \cdot 2 \cdot 9} T_0 = \frac{15}{18} T_0$

$A'(T) = \frac{9}{10} \frac{R}{T_0} 2T - \frac{3}{2} R$

$A'(T) = 0 : \frac{18}{10} \frac{R T}{T_0} - \frac{15}{2} R = 0$

$\frac{18 R T}{10 T_0} = \frac{15 R}{2}$

$T = \frac{15}{18} T_0$

3)  $A_{min}$

$A_{min} = A(T = \frac{15}{18} T_0) = \frac{9}{10} \frac{R}{T_0} \left( \frac{15^2}{18^2} T_0^2 - T_0^2 \right) - \frac{3}{2} R \left( \frac{15}{18} T_0 - T_0 \right) =$

# Часть 2

Олимпиада: **Физика, 11 класс (2 часть)**

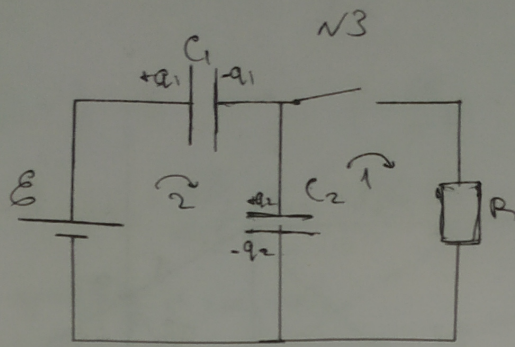
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Вариант 4

$C_2 = C$   
 $C_1 = 5C$

- 1)  $\Sigma_{R_1} = ?$   
 2)  $Q = ?$   
 3)  ~~$\Sigma_{R_1}$~~   
 $\Sigma_{R_1}; \Sigma_{R_2} = ?$



1) Сразу после замыкания  
 $\uparrow U_R - U_{C2} = 0$  — правило Кирхгофа

$\Sigma_{R_1} R = U_{C2}$

$\Sigma \rightarrow \varepsilon = U_{C1} + U_{C2}$

Закон сохранения заряда (кнопка ~~была~~ разомкнута):

$q_2 - q_1 = 0 \quad q_2 = q_1 \quad ; \quad U_{C1} = \frac{q_1}{C_1} \quad , \quad U_{C2} = \frac{q_2}{C_2} = \frac{q_1}{C_2}$

$\varepsilon = q_1 \left( \frac{1}{C_1} + \frac{1}{C_2} \right) = q_1 \frac{\varepsilon}{5C} \quad ; \quad q_1 = \frac{5}{6} \varepsilon C \quad ; \quad U_{C2} = \frac{5}{6} \frac{\varepsilon C}{C} = \frac{5}{6} \varepsilon$

$\Sigma_{R_1} = \frac{U_{C2}}{R} = \frac{5}{6} \frac{\varepsilon}{R}$

$U_{C1} = \frac{1}{6} \varepsilon$

2)  $A_{\text{ист}} - Q = W_2 - W_1$

$W_1 = \frac{C_1 U_1^2}{2} + \frac{C_2 U_2^2}{2} \quad ; \quad W_2 = \frac{C_1 U_3^2}{2} + \frac{C_2 U_4^2}{2}$

Конденсатор 1 заряжен до  $U_3 = \varepsilon$ , а конденсатор 2 разряжен через резистор

$A_{\text{ист}} = \Delta q_1 \varepsilon = (q_3 - q_1) \varepsilon = (\varepsilon C_1 - U_1 C_1) \varepsilon = \varepsilon^2 (5C - \frac{5}{6}C) = \frac{25}{6} \varepsilon^2 C$

$U_4 = 0$

$Q = W_2 - W_1 + A_{\text{ист}} = \frac{5C(\frac{1}{6}\varepsilon)^2}{2} + \frac{C(\frac{5}{6}\varepsilon)^2}{2}$

$Q = \frac{5C\varepsilon^2}{2} + 0 - \frac{5C(\frac{1}{6}\varepsilon)^2}{2} - \frac{C(\frac{5}{6}\varepsilon)^2}{2} + \frac{25}{6} \varepsilon^2 C = \frac{5}{2} C \varepsilon^2 - \frac{5}{72} C \varepsilon^2 - \frac{25}{72} C \varepsilon^2 + \frac{25}{6} C \varepsilon^2 =$

$= C \varepsilon^2 \left( \frac{100}{72} + \frac{25}{6} \right) \approx 6,25 C \varepsilon^2$

Ответ: 1)  $\Sigma_{R_1} = \frac{5}{6} \frac{\varepsilon}{R} \quad ; \quad 2) Q = 6,25 C \varepsilon^2$



$$B, L, \nu_0$$

$$m_1, 2Rm$$

$$m_2 = \frac{m}{2}$$

$$R_1 = R$$

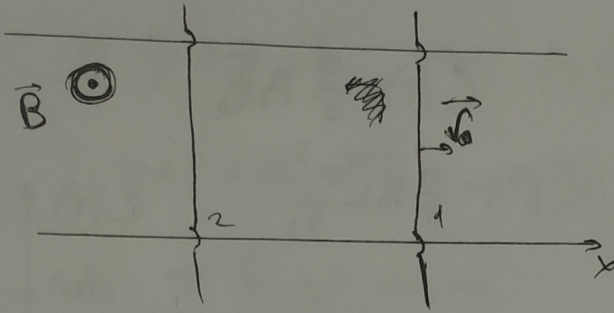
$$R_2 = 5R$$

$$1) a_1 = ?$$

$$2) \nu_1, \nu_2 = ?$$

$$3) \Delta L = ?$$

N4



$$1) \mathcal{E}_0 = \frac{d\Phi_B}{dt} = \frac{BdS}{dt} = \frac{BLdv}{dt} = BL\nu_0$$

но контур имеет резисторы

$$\mathcal{E}_0 = \mathcal{I}_0 R_2 + \mathcal{I}_0 R_1, \quad \mathcal{I}_0 = \frac{\mathcal{E}_0}{R_1 + R_2}$$

$$\mathcal{I}_0 = \frac{\mathcal{E}_0}{6R}$$

$$R_3. \text{ Короткая на об. } m_1 a_1 = F_A; \quad F_A = \mathcal{I}_0 L B$$

$$m_1 a_1 = \frac{\mathcal{E}_0}{6R} L \cdot B, \quad a_1 = \frac{BL\nu_0}{6Rm_1} \cdot LB, \quad a_1 = \frac{B^2 L^2 \nu_0}{12Rm}$$

2) направление тока определяется, с.н. по правилу правой руки

$$\text{Ответ: } 1) a_1 = \frac{B^2 L^2 \nu_0}{12Rm}$$

v5

$$R = 24 \text{ см}$$

$$M = 9 \text{ см}$$

$$d = L_1 = 26 \text{ см}$$

$$L_2 = 24 \text{ см}$$

x = ?

 $D_M = ?$  $L_3 = ?$ 

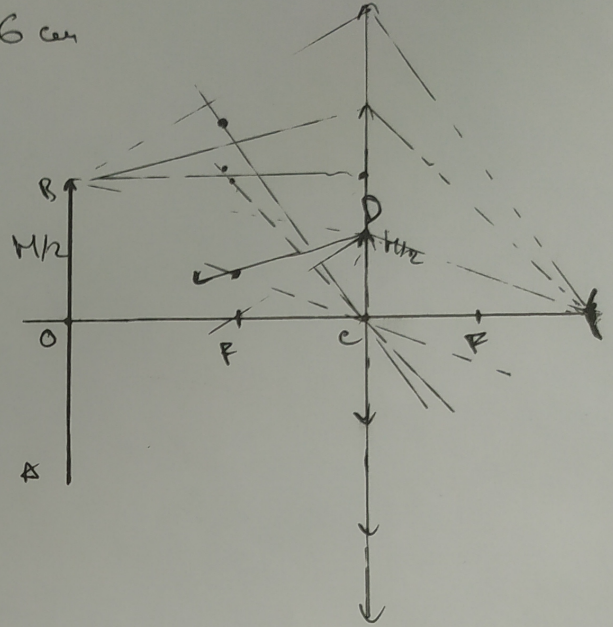
$$1) \frac{1}{d} + \frac{1}{f} = \frac{1}{R} \quad \Leftrightarrow \quad f = \frac{dR}{d-R} = 32 \text{ см}$$

$$x = f + L_2 = \frac{dR}{d-R} + L_2 = 56 \text{ см}$$

2) при  $D_M \leq M$  изображение будет узкое.

$$D_M = \frac{M}{f} + 1$$

$$D_M = 2$$



Ответ: 1)  $x = \frac{dR}{d-R} + L_2 = 56 \text{ см}$



Бапурац у-а

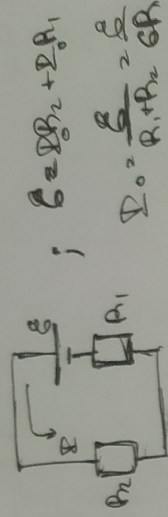
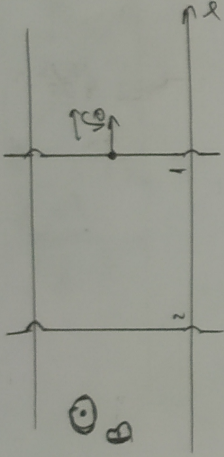
Урпнебух

21202524 (U319163 M1266891)

$L_1, L_2$
$m_1, m_2, R_1, R_2$
$m_1 v_1, m_2 v_2, R_1, R_2, v_0$
$v_0, B$
1) $a_1, a_2$
2) $v_1, v_2$
3) $v_0$

NS

$$1) \mathcal{E} = \frac{d\Phi_B}{dt} = \frac{B L dx_2}{dt}$$



$$F_A = R_1 I_1 B = \frac{\mathcal{E}}{R_1} v_0 B$$

$$m a_1 = F_A; \quad a_1 = \frac{F_A}{m_1} = \frac{\mathcal{E} v_0 B}{R_1 m_1} = \frac{1}{2} \mathcal{E} v_0 B$$

$$2) \text{ЗСМ: } \frac{m_1 v_0^2}{2} = \frac{m_2 v_2^2}{2} + \frac{m_1 v_1^2}{2}$$

$$\text{ЗСМ: } m_1 v_0 = m_1 v_1 + m_2 v_2$$

$$\Leftrightarrow \left\{ \begin{aligned} \frac{2m_1 v_0^2}{2} &= \frac{m_1 v_1^2}{2} + \frac{2m_2 v_2^2}{2} \\ 2m_1 v_0 &= 2m_1 v_1 + 2m_2 v_2 \end{aligned} \right. \Rightarrow \left\{ \begin{aligned} v_2 &= v_1 - v_0 \\ v_2^2 &= v_1^2 - v_0^2 \end{aligned} \right.$$

$$\left. \begin{aligned} 4v_0^2 &= 4v_1^2 + v_2^2 \\ 4v_0 &= 4v_1 - v_2 \end{aligned} \right\} \Leftrightarrow \left\{ \begin{aligned} v_2 &= v_1 - v_0 \\ v_2^2 &= 4(v_0^2 - v_1^2) \end{aligned} \right.$$

$$v_2 = \frac{(v_0 - v_1)(v_0 + v_1)}{(v_1 - v_0)} = -v_0 - v_1$$

$$4v_0^2 = 4v_1^2 + 16(v_1 - v_0)^2$$

$$4v_0^2 = 4v_1^2 + 16v_1^2 - 32v_1 v_0 + 16v_0^2$$

$$-v_0 - v_1 = 4v_1 - 4v_0 \quad \Rightarrow \quad 3v_0 = 5v_1$$

$$R_2 = 4 \cdot \frac{2}{5} v_0 = v_2 = 4 \left( \frac{3}{5} v_0 - v_0 \right) = -\frac{8}{5} v_0$$

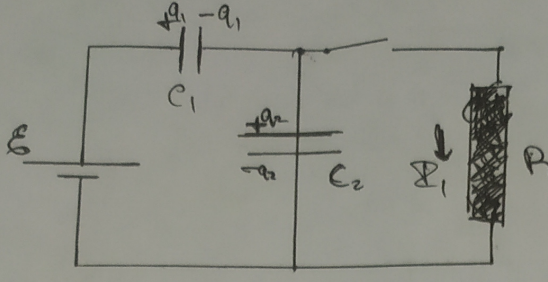
$$4 \cdot v_0^2 = 4 \cdot \frac{9}{25} v_0^2 + \frac{64}{25} v_0^2$$

5)

1)

$C_1 = 5C$   
 $C_2 = C$

- 1)  $\Phi_A$  -?
- 2)  $Q$  -?
- 3)  $\Phi_R$  -?



1)  $\mathcal{E} = U_1 + U_2$   
 $\mathcal{E} = \frac{q_1}{C_1} + \frac{q_2}{C_2}$   
 $q_1 = q_2 = q_0$

$\mathcal{E} = \frac{q_0}{5C} + \frac{q_0}{C} ; \mathcal{E} = \frac{6}{5} \frac{q_0}{C}$

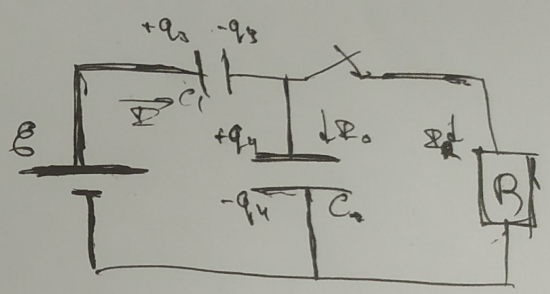
~~$U_1 = \frac{q_0}{C_1} = \frac{5}{6} \frac{\mathcal{E}}{5} = \frac{\mathcal{E}}{6}$~~   
 $\frac{U_1}{U_2} = \frac{C_2}{C_1} = \frac{1}{5}$

$U_1 = \frac{q_0}{C_1} = \frac{1}{6} \frac{6q_0}{5C} = \frac{1}{6} \frac{5\mathcal{E}}{5} = \frac{\mathcal{E}}{6}$   
 $U_2 = \frac{5}{6} \mathcal{E}$

$\Phi_R = U_2 ; \Phi_R = \frac{U_2}{R} = \frac{5}{6} \frac{\mathcal{E}}{R}$

2)  $A_{\text{ист}} = Q = W_2 - W_1$

$W_1 = \frac{C_1 U_1^2}{2} + \frac{C_2 U_2^2}{2} ;$



3)  $\mathcal{E} = U_1 + I_R R$

$I_R R = U_2 ; U_2 = \frac{q_4}{C_2}$

15

$R = 24 \text{ cm}$

$M = 9 \text{ cm}$

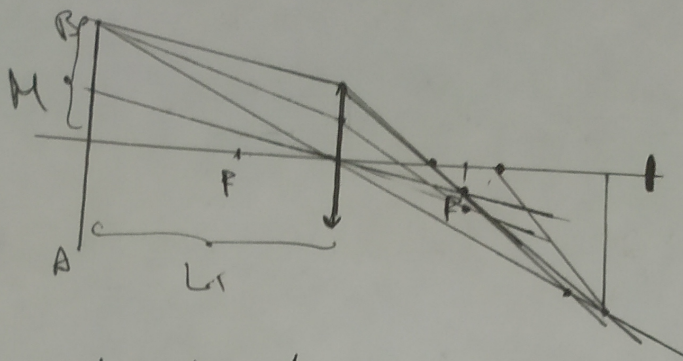
$d = L_1 = 96 \text{ cm}$

$L_2 = 24 \text{ cm}$

1)  $X = ?$

2)  $D_M = ?$

3)  $L_3 = ?$



1)  $\frac{1}{d} + \frac{1}{f} = \frac{1}{R}$

$f = \frac{dR}{d-R} = \frac{96 \cdot 24}{96-24} = 32 \text{ cm}$

$X = f + L_2 = 32 + 24 = 56 \text{ cm}$

$\Gamma = \frac{f}{d} = \frac{32}{96} = \frac{1}{3}$

2)  ~~$f_2 = 56 \text{ cm}$~~

~~$R_2 = \frac{56}{32} = 1.75$~~

