

Часть 1

Олимпиада: **Физика, 9 класс (1 часть)**

Шифр: **21204181**

ID профиля: **360362**

Вариант 2

Задача 1

Дано:

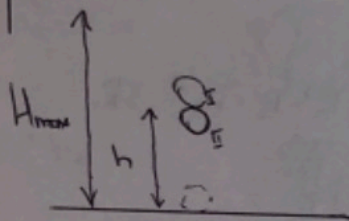
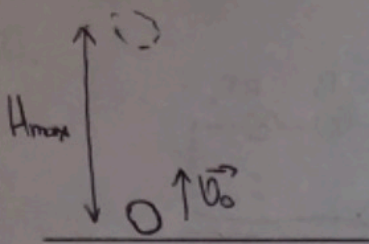
τ

$v_0 = v_0$

$\tau_1 = ?$

$H_{max} = ?$

$v_0 = ?$



Анализ и решение:

$$3(\tau): \frac{mv_0^2}{2} = mgh$$

$$\tau = \tau_1 + \tau_2$$

где τ_1 - для тела I на высоте H_{max}

τ_2 - для тела II на высоте h

$$h = \frac{g\tau_1^2}{2} \rightarrow h = \frac{g\tau^2}{2}; H = \frac{g\tau^2}{2}$$

$$H = \frac{v_0^2}{2g} \Rightarrow v_0 = \sqrt{2gH}$$

$$\frac{g\tau_1^2}{2} + (v_0\tau_2 - \frac{g\tau_2^2}{2}) = H \rightarrow \tau_2 = \frac{H}{v_0}$$

$$\tau_2^2 = \frac{H^2}{v_0^2} = \frac{H}{2g} = \frac{g\tau^2}{2} \cdot \frac{1}{2g} \Rightarrow 2\tau_2 = \tau$$

$$\tau = 3\tau_2 \Rightarrow \tau_2 = \frac{\tau}{3} \Rightarrow \tau_1 = \frac{2}{3}\tau \Rightarrow \tau_1^2 = \frac{4}{9}\tau^2$$

$$H = \frac{4}{9}\tau^2 \cdot g = \frac{2g\tau^2}{9}$$

$$v_0 = \sqrt{2gH} = \sqrt{2g \cdot \frac{2g\tau^2}{9}} = \sqrt{\frac{4g^2\tau^2}{9}} = \frac{2g\tau}{3}$$

Ответ: $\tau_1 = \frac{2}{3}\tau$; $H = \frac{2}{9}g\tau^2$; $v_0 = \frac{2}{3}g\tau$



Чистовик Вариант 09-0,2

2

Дано:

$$S = 9 \cdot 10^{-4} \text{ м}^2$$

$$m = 0,25 \text{ кг}$$

$$H = 0,2 \text{ м}$$

$$M : p - ?$$

$$m = \frac{M}{10}$$

$$h - ?$$

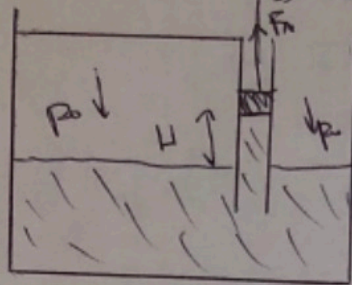
$$p_0 = 1 \cdot 10^5 \text{ Па}$$

$$\rho = 1000 \frac{\text{кг}}{\text{м}^3}$$

$$g = 10 \frac{\text{м}}{\text{с}^2}$$

Анализ и решение:

①



$$p = \frac{F}{S}$$

$$p = \rho g H = 2000 \text{ (Па)}$$

$$\rho g H + \frac{mg}{S} = p_0 + \frac{Mg}{S}$$

$$\rho g HS + mg = p_0 S + Mg$$

$$M = \frac{\rho g HS + mg - p_0 S}{g}$$

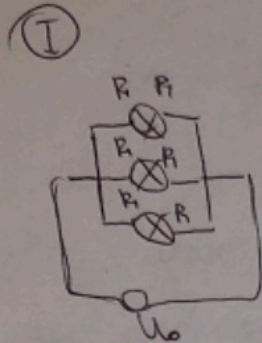
$$M = \frac{1000 \cdot 10 \cdot 0,2 \cdot 9 \cdot 10^{-4} + 0,25 \cdot 10 - 10^5 \cdot 9 \cdot 10^{-4}}{10}$$

$$M = 1,8 + 2,5$$

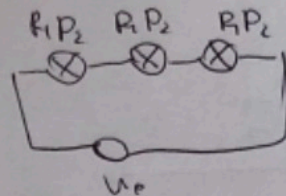
3
 Дано:
 $U_0 = 6\text{В}$
 $P_1 = 2,4\text{Вт}$
 $P_2 = 0,5\text{Вт}$

 $I = ?$
 $U_{02} = \frac{U_0}{3}$
 $P_1' = ?$

Анализ и решение:



(II)



(I) $P_1 = \frac{U^2}{R_1} \Rightarrow R_1 = \frac{U^2}{P_1}$

(II) $P_2 = I^2 R_1$

$\frac{1}{R} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3}; U = U_1 = U_2 = \dots$

$R = R_1 + R_2 + R_3 = 3R_1$

$R = \frac{R_1}{3}$

$I = \sqrt{\frac{P_2}{R_1}}$

$I_1 = I_2 = I_3 = \sqrt{\frac{P_2}{R_1}} = \sqrt{\frac{0,5}{15}} = 0,183\text{А}$

$I_1 = \frac{U}{R_1} = \frac{4P_1}{U^2} = \frac{P_1}{U}$

(III) $P_1' = \frac{U_{02}}{R_1} = \frac{U_0}{3R_1}$

$P = P_1 + P_2 + P_3 = 3P_1$

$I_1 = 0,4\text{А}$

т.к. лампы одинак.

$R_1 = R_2 = R_3$

$u P_1 = P_2 = P_3$

$P_1' = \frac{6\text{В}}{3 \cdot 15\text{Ом}}$

$P_1' = 0,133\text{Вт}$

$I_2 = \frac{U}{R_2}; P_2 = \frac{U^2}{R_2} \Rightarrow I_2 = \frac{U}{R_2} = \frac{P_2}{U}$

$I_3 = \frac{P_3}{U}$

$I_1 = I_2 = I_3 = 0,4\text{А} \Rightarrow$

$\Rightarrow R_1 = \frac{U}{I_1} = 150\text{Ом}$

Ответ: (I) $I = 0,4\text{А}$ (II) $I = 0,183\text{А}$; (III) $P_1' = 0,133\text{Вт}$

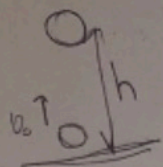
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Церковник

Вариант 09-02

①

$$h = \frac{g\tau^2}{2}$$

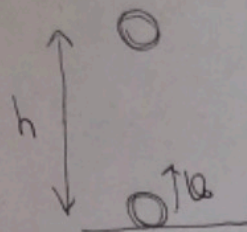


$$\tau = \tau_1 + \tau_2$$

$$v_{\tau_1} = v_0 - g\tau = 0 \Rightarrow v = g\tau$$

$$\frac{mv^2}{2} = mgh$$

$$v^2 = 2gh$$



$$\tau_2 = \tau - \tau_1$$

$$h = \frac{v_0^2}{2g} \quad \text{mgH} = mgh + \frac{mv^2}{2}$$

$$h = \frac{g\tau^2}{2}$$

$$H = g\tau_1^2$$

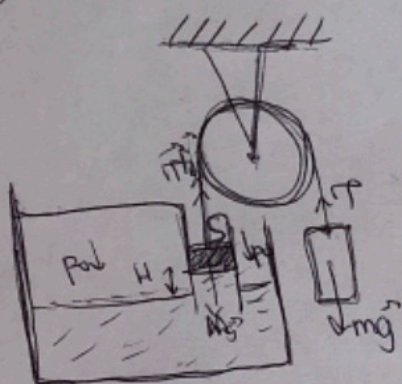
$$H = v_0\tau_2 - 2g\tau_2^2$$

$$\tau_2 = \sqrt{\frac{H}{2g}}$$

$$v^2 = 2g \cdot g\tau^2$$

$$v_0^2 = g^2\tau^2 \Rightarrow v = g\tau \Rightarrow \tau = \frac{v}{g}$$

②



$$p = \frac{F}{S} \Rightarrow F = p \cdot S$$

$$mg = F_2$$

$$10000 \cdot 0,2 = 2000$$

$$p_0 + \frac{mg}{S} = p_0H + \frac{Mg}{S}$$

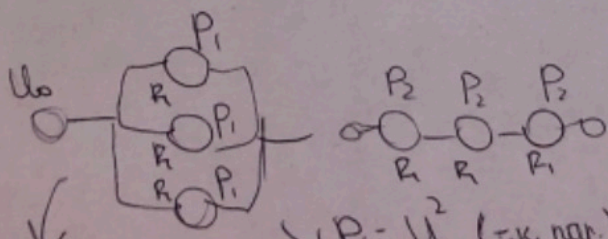
$$p_0S + mg = p_0HS + Mg$$

$$M = \frac{p_0S \cdot mg - p_0HS}{g}$$

$$p_0 = \frac{p_0HS + Mg}{S}$$

$$p_0 = 9 \cdot 10^4 \cdot 1 \cdot 10^{-5}$$

③



$$3P_2 = I^2 R \quad \frac{5}{150} = \frac{1}{30}$$

$$P_2 = I^2 R \quad (\text{т.к. } R \text{ одинаков})$$

$$P_1 = \frac{U^2}{R} \quad (\text{т.к. } U \text{ одинаков})$$

$$\frac{1}{R} = \frac{1}{R} + \frac{1}{R} + \frac{1}{R} \Rightarrow R = \frac{R}{3}$$

$$R = \frac{U^2}{P_1}$$

$$I_1 = \frac{U}{R}$$

$$I = \frac{U}{R}$$

$$2 \frac{5}{10} = 2 \frac{5}{10} = \frac{10}{10}$$

$$R = \frac{U}{I}$$

$$R = \frac{5}{36}$$

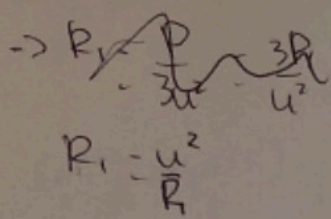
$$U P_1 \Rightarrow I_1 = U P_1 = 6 \cdot 2,4$$

$$\frac{14,4}{14,4} = 1$$

$$\frac{6}{14,4} = \frac{1}{2,4}$$

Цепиобар

$$\textcircled{3} P = \frac{U^2}{R} = \frac{3U^2}{R} \quad I = I_1 + I_2 + I_3$$



$$P = I^2 R$$

$$3P_1 = I^2 R$$

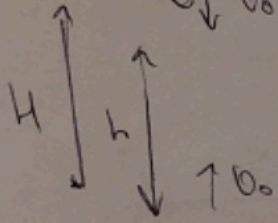
$$916 \cdot 15$$

$$I = 9I_1$$

$$3I_1^2 R = P_1$$

$$\textcircled{4} \tau_2^2 = \frac{H}{2g} = \frac{g\tau_1^2}{2g} \rightarrow 4\tau_2^2 = \tau_1^2$$

$$2\tau_2 = \tau_1$$



$$v_0 \tau_2 - g \frac{\tau_2^2}{2} = h$$

$$g \frac{\tau_2^2}{2} = H - h$$

$$(I) + (II) = H$$

$$v_0 \tau_2 = H = g \frac{\tau_2^2}{2}$$

$$2v_0 \tau_2 = g \tau_2^2$$

$$\tau_2^2 = \frac{H^2}{v_0^2} = \frac{H^2}{2gH} = \frac{H}{2g} = g \frac{\tau_1^2}{2} \cdot \frac{1}{2g}$$

$$4\tau_2^2 = \tau_1^2 \rightarrow \tau_1 = 2\tau_2$$

Часть 2

Олимпиада: **Физика, 9 класс (2 часть)**

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ID профиля: **360362**

Вариант 2

IV

Числовик

09.02

Дано:

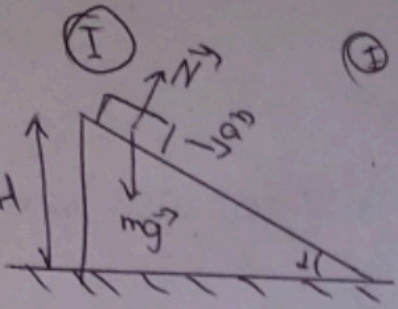
$m = m$

$M = 2m$

$l; H$

$\tau, ?$

$a_2; t, ?$



Анализ и решение:

I $\sin \alpha = \sqrt{1 - \cos^2 \alpha} = \frac{4}{5}; l = \frac{H}{\sin \alpha}$

II закон Ньютона:

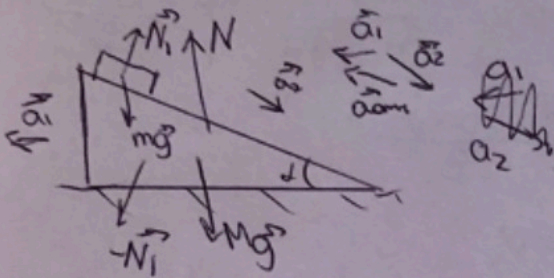
$mg \sin \alpha = ma \rightarrow a = g \sin \alpha$

BCD: $v^2 = 2gH$

$\sqrt{2gH} = a\tau = g \sin \alpha \cdot \tau \Rightarrow \tau = \sqrt{\frac{2H}{g}} \cdot \frac{1}{\sin \alpha}$

$\tau = \frac{\sqrt{5H}}{4} (c)$

II



$a_1 = g \frac{\cos \alpha \sin \alpha}{2 + \sin^2 \alpha} \Rightarrow$

$\Rightarrow a_{\text{com}} = \frac{(m+M) \sin \alpha}{M + m \sin^2 \alpha} \cdot g \Rightarrow$

$\Rightarrow \text{т.к. } \frac{a_{\text{com}} \tau^2}{2} = \frac{H}{\sin \alpha}$

$\tau = \sqrt{\frac{2H}{a_{\text{com}} \sin \alpha}}$

$\tau = \sqrt{\frac{2H(M + m \sin^2 \alpha)}{\sin^2 \alpha g (M + m)}} = \frac{2H \cdot m (2 + \sin^2 \alpha)}{m \sin^2 \alpha \cdot g (2 + 1)} = \sqrt{\frac{2H(\sin^2 \alpha + 2)}{\sin^2 \alpha g \cdot 3}}$

$a_1 = \frac{10 \cdot \frac{3}{5} \cdot \frac{4}{5}}{2 + \frac{16}{25}} = \frac{\frac{120}{25}}{\frac{66}{25}} = \frac{120}{66} = \frac{20}{11} \approx 1,81 \text{ м/с}^2$

$\tau = \sqrt{\frac{2H(\frac{16}{25} + 2)}{\frac{16}{25} \cdot 10 \cdot 3}} = \sqrt{\frac{2H \cdot \frac{66}{25}}{19,2}} = \sqrt{0,275H} \approx 0,5244 \sqrt{H} (c)$

Ответ: I $\tau = \frac{\sqrt{5H}}{4} c$; II $a_1, 21,81 \text{ м/с}^2; \tau = 0,5244 \sqrt{H} c$

⑤

②

Дано:

$H; S$

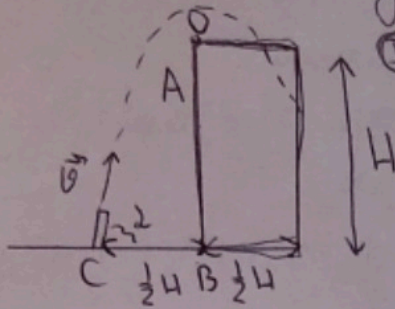
$v = \sqrt{2,5gH}$

$\tau = ?$

$\alpha = ?$

$g = 10 \text{ м/с}^2$

Дування у рішечині



①

$m = \rho \cdot V$

$V = H \cdot S, = H \cdot \frac{\pi R^2}{2} \Rightarrow 0,03125 H^3 \cdot \rho \cdot \pi = m$

$m = \rho \cdot v \cdot \tau \cdot S$

$0,03125 H^3 \cdot \rho \cdot \pi = \rho \cdot v \cdot \tau \cdot S$

$\tau = \frac{0,03125 \cdot H^3 \cdot \pi}{v \cdot S} = \frac{0,03125 \cdot H^3 \cdot \pi}{S \cdot \sqrt{2,5gH}} = \frac{0,00625 \cdot H^3 \cdot \pi}{S \cdot \sqrt{H}}$

$\tau = \frac{\sqrt{H} \cdot H^2 \cdot 0,00625 \cdot \pi}{S} = \frac{\sqrt{H^5} \cdot 0,00625 \cdot \pi}{S}$

②

сфера падає в точку O при $\alpha = 60^\circ$

$\Delta ABC; \angle CBA = 90^\circ$ у $OB = H; CB = \frac{1}{2}H \rightarrow \angle CAB = 30^\circ \rightarrow$

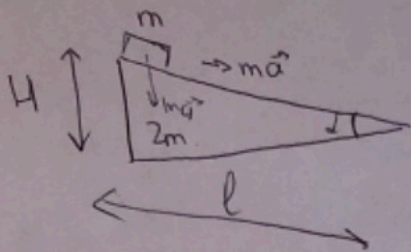
\Rightarrow при $\alpha = 60^\circ$ сфера падає в точку A. при $v = \sqrt{2,5gH}$

③

~~1/4 H~~ $2gH_1 = 2,5gH \Rightarrow H_1 = \frac{5}{4}H$

Черный

Ⓜ



2.64 $\frac{16 \cdot 6}{5}$ 0.64

$\frac{16 \cdot 30}{25}$ mg 19.2

Ⓜ $mgH = \frac{mV^2}{2} + \frac{Mu^2}{2}$

$mV = Mu \Rightarrow V = \frac{Mu}{m}$

$mgH = \frac{m \cdot M^2 \cdot u^2}{2m^2} + \frac{Mu^2}{2}$

$2m^2gH = M^2u^2 + mM u^2$

$u^2 = \frac{2m^2gH}{M(m+M)} \Rightarrow u = m \sqrt{\frac{2gH}{M(m+M)}}$

$mg \cos \alpha = Ma$

$u = a \cdot \tau$

Ⓜ $V^2 = 2gH \frac{1}{\sin^2 \alpha} = g \sin \alpha \cdot \tau$

$2gH \sin \alpha \cdot \tau = u^2$

$\tau = \frac{1}{2g \sin \alpha}$; $H = g \sin^2 \alpha \cdot \tau^2$
 $\tau = \sqrt{\frac{H}{g \sin^2 \alpha}}$

$\sin \alpha = \frac{H}{l}$ $\sin \alpha = \frac{H}{l}$

$\sin \alpha = \sqrt{1 - \cos^2 \alpha} = \sqrt{1 - \frac{y^2}{25}} = \frac{4}{5}$

Ⓜ $mgH = \frac{mV^2}{2} \Rightarrow H = \frac{V^2}{2g}$

$mg \sin \alpha = ma \Rightarrow g \sin \alpha = a$

$V = at = g \tau \sin \alpha = \frac{l}{\tau}$

$\sqrt{2gH} = \frac{l \cdot \sin \alpha}{\tau}$

$\tau = \sqrt{\frac{2H}{g}} \sin \alpha$

$2gH = g \tau^2 \sin^2 \alpha$

$\sqrt{2gH} = \tau \sin \alpha \cdot g$

$\sqrt{\frac{2H}{g}} \sin \alpha = \tau$

$g \tau^2 \sin^2 \alpha = H \sin \alpha$

$g \sin \alpha \cdot \tau = \frac{H \sin \alpha}{\tau}$

$\tau = \sqrt{\frac{H}{g}}$

$mgH = \frac{mV^2}{2} \Rightarrow V = \sqrt{2gH} = g \sin \alpha \cdot \tau$

$\tau = \sqrt{\frac{2H}{g}} \sin \alpha$

$l = \frac{a \tau^2}{2}$

$\frac{H}{\sin \alpha} = g \frac{\tau^2}{2}$

$\tau \sqrt{2gH} = \frac{H \cdot \sin \alpha}{\tau}$

$= \frac{H \sin \alpha}{\tau}$

$V = \sqrt{2gH} = \frac{H}{\sin \alpha \cdot \tau} = g \sin \alpha \cdot \tau$

$\tau = \sqrt{\frac{2gH \cdot \sin \alpha}{H}}$

$\sqrt{2gH} = g \sin \alpha \cdot \tau \Rightarrow \tau = \frac{\sqrt{2gH}}{g \sin \alpha}$

$H = g \sin^2 \alpha \cdot \tau^2 \Rightarrow \tau = \sqrt{\frac{H}{g \sin^2 \alpha}}$

Черников

Вариант 09-02

IV

Черников

Дано:

$m = m$

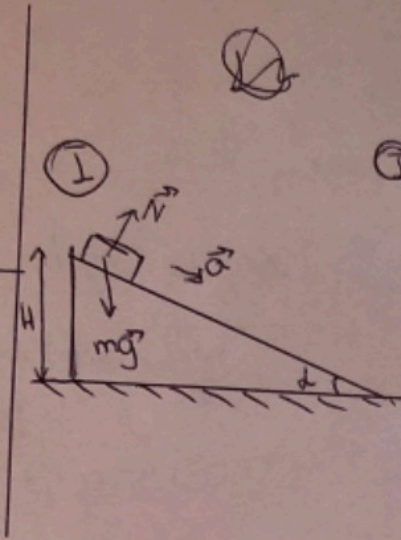
$M = 2m$

$l; H$

$\tau - ?$

$a_2; t - ?$

$\cos \alpha = \frac{3}{5}$



Анализ и решение:

① $v_0 = 0 \Rightarrow v = at = l$

$\sin \alpha = \sqrt{1 - \cos^2 \alpha} = \frac{4}{5}$

II закон Ньютона:

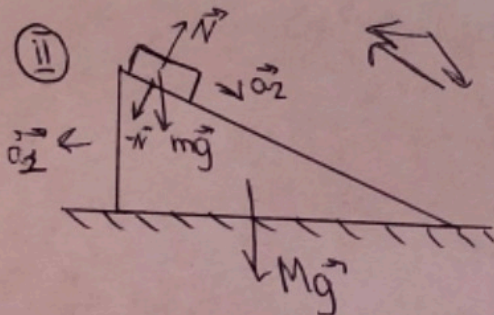
$mg \sin \alpha = ma \Rightarrow a = g \sin \alpha$

ЗСЭ: $mgH = \frac{mv^2}{2} \Rightarrow v^2 = 2gH$

$l = \frac{v^2}{2a} = \frac{2gH}{2g \sin \alpha} = \frac{H}{\sin \alpha}$

$\tau = \sqrt{\frac{2H}{g}} \cdot \frac{1}{\sin \alpha}$

$\tau = \sqrt{\frac{H}{5}} \cdot \frac{5}{4} = \frac{\sqrt{5H}}{4} \text{ (с)}$



② $m\vartheta = Mu \Rightarrow \vartheta = \frac{Mu}{m}$

$mgH = \frac{Mu^2}{2} + \frac{m\vartheta^2}{2}$

$2m^2gH = M^2u^2 + mM\vartheta^2 \Rightarrow u = m \sqrt{\frac{2gH}{M(m+M)}} \Rightarrow \vartheta = M \sqrt{\frac{2gH}{M(m+M)}}$

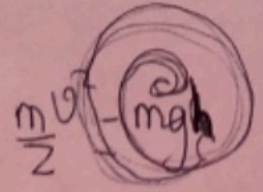
~~$N = mg \cos \alpha \Rightarrow N_1 = mg \cos \alpha \cdot \sin \alpha = Mg \sin \alpha \Rightarrow a_1 = \frac{mg \cos \alpha \sin \alpha}{M}$~~

~~$a_1 = a_2 \sin \alpha \Rightarrow a_2 = a_1 \sin \alpha$~~

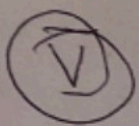
~~$M a_1 = N \sin \alpha$~~
 ~~$M a_2 = N + \dots$~~

$\vec{a}_2 = \vec{a}_{\text{cm}} + \vec{a}$

V

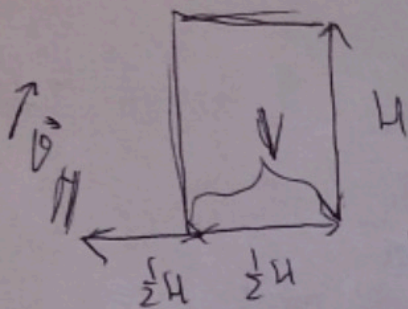


$\vartheta = \sqrt{2gH}$



Черный.

09-02



$$v = \sqrt{2,5gH}$$

$$dm = \rho \cdot v \cdot S \cdot dt$$

$$m = \rho V$$

$$V = HS$$

~~$$m = \rho \cdot v \cdot S \cdot dt$$~~

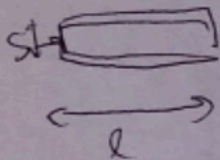
$$\frac{mv^2}{2} = mgH \quad v^2 = 2gH$$

$$2,5gH = 2gH$$

$$S = \frac{\pi R^2}{2} = 0,0625 \frac{H^2}{2} \pi = 0,03125 H^2 \pi$$

$$0,5H = 0,4H$$

$$v \cdot S = \pi$$



~~$$m = \rho \cdot H^3 \pi \cdot 0,03125$$~~

$$5H = 4H$$

$$H_1 = \frac{1}{4} H$$

$$l = v \cdot \tau \rightarrow m = v \cdot \tau \cdot S \cdot \rho$$